



Carnegie Mellon University
Computer Science Department



Estimating Node Importance in Knowledge Graphs Using Graph Neural Networks

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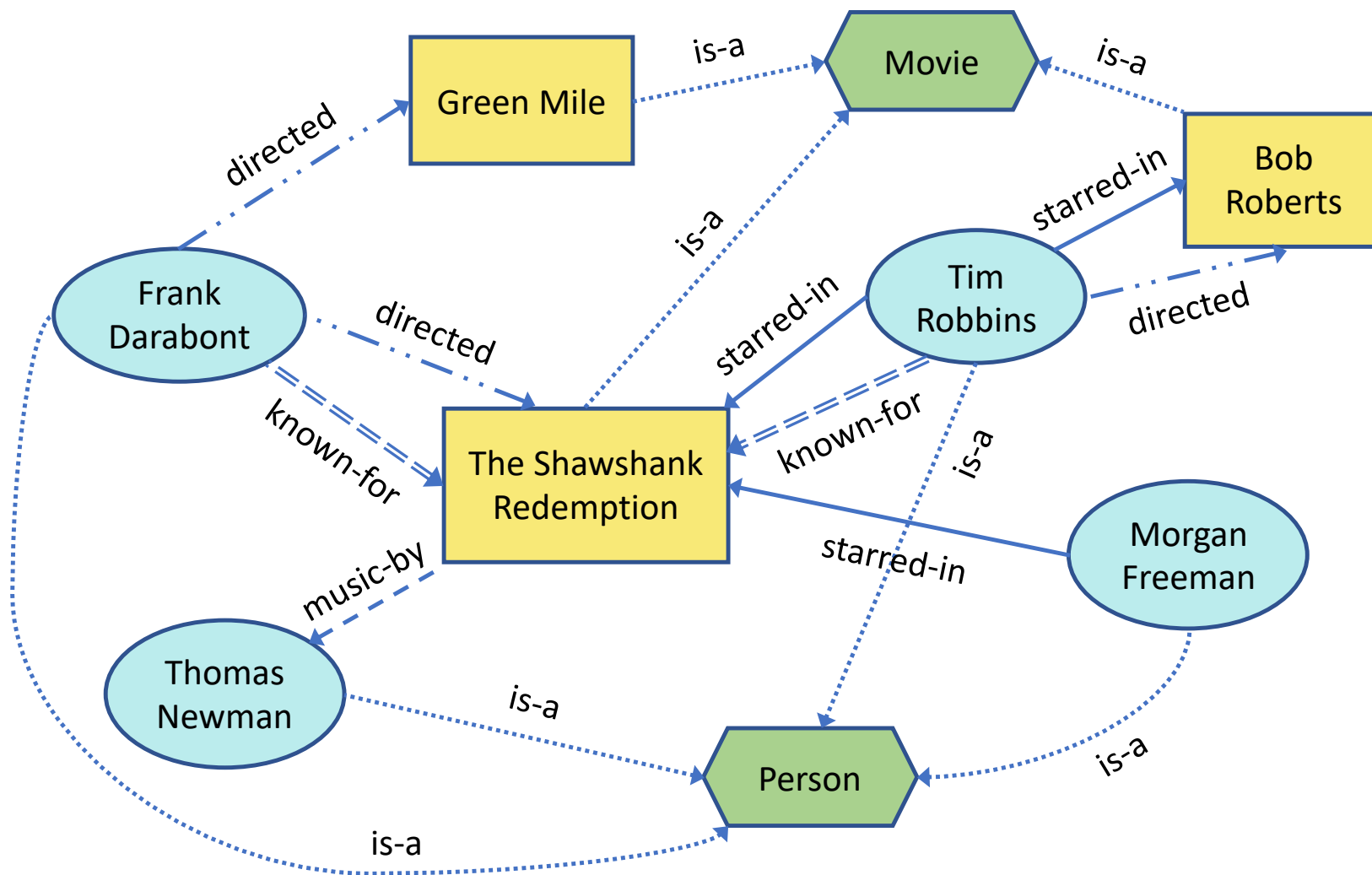


Roadmap

- **Introduction**
 - Knowledge Graph
 - Problem Definition
 - Existing Methods
- Proposed Method: GENI
- Experimental Results
- Conclusion

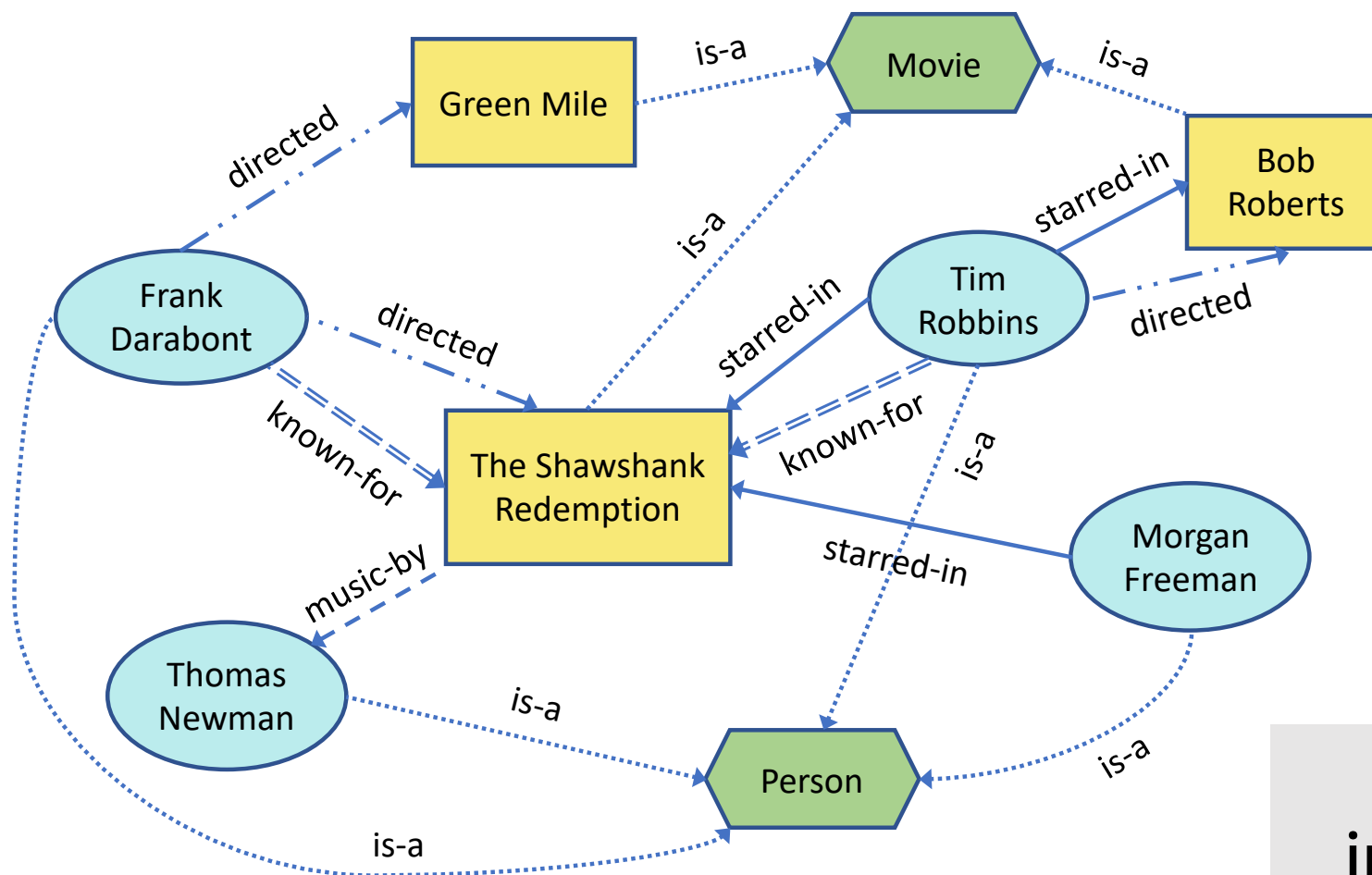


Knowledge Graph



An example knowledge graph on movies and related entities

Node Importance



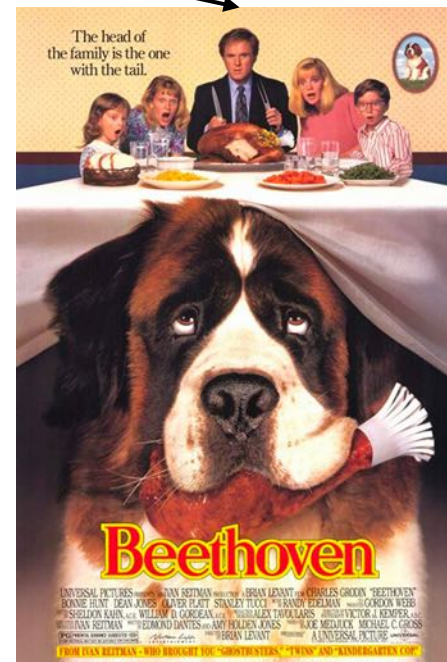
Most important directors

What are the most important nodes in a KG?

Applications

Query disambiguation

“Beethoven”



Applications



- Search
- Information extraction



- Quality control for KGs

* Image source: www.freepik.com

Importance Score

- Often we can observe a signal that indicates node importance
- Examples



Total gross



Number of votes

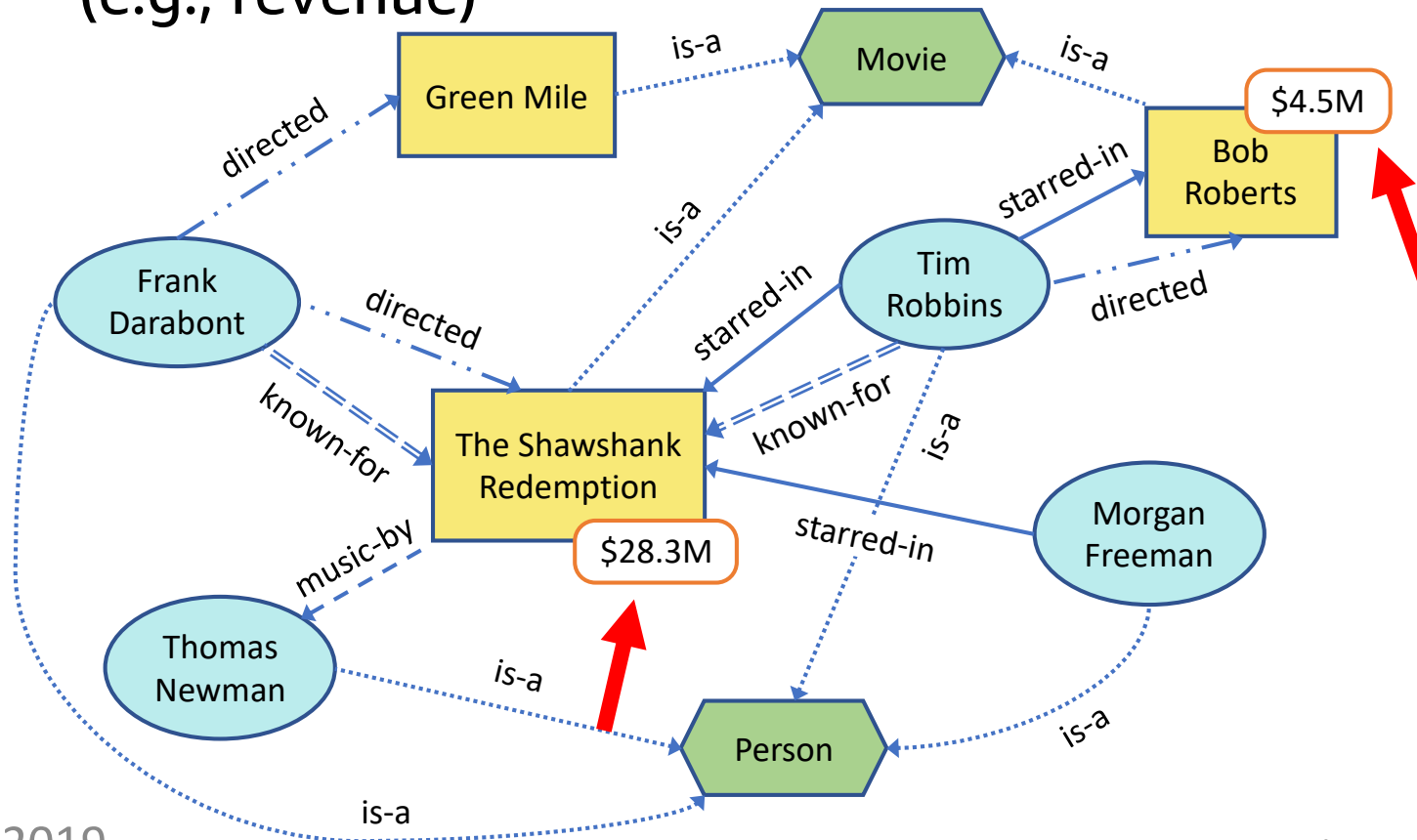


Number of pageviews

Node Importance Estimation

Input

- A knowledge graph
- Input scores for some nodes (e.g., revenue)



Node Importance Estimation

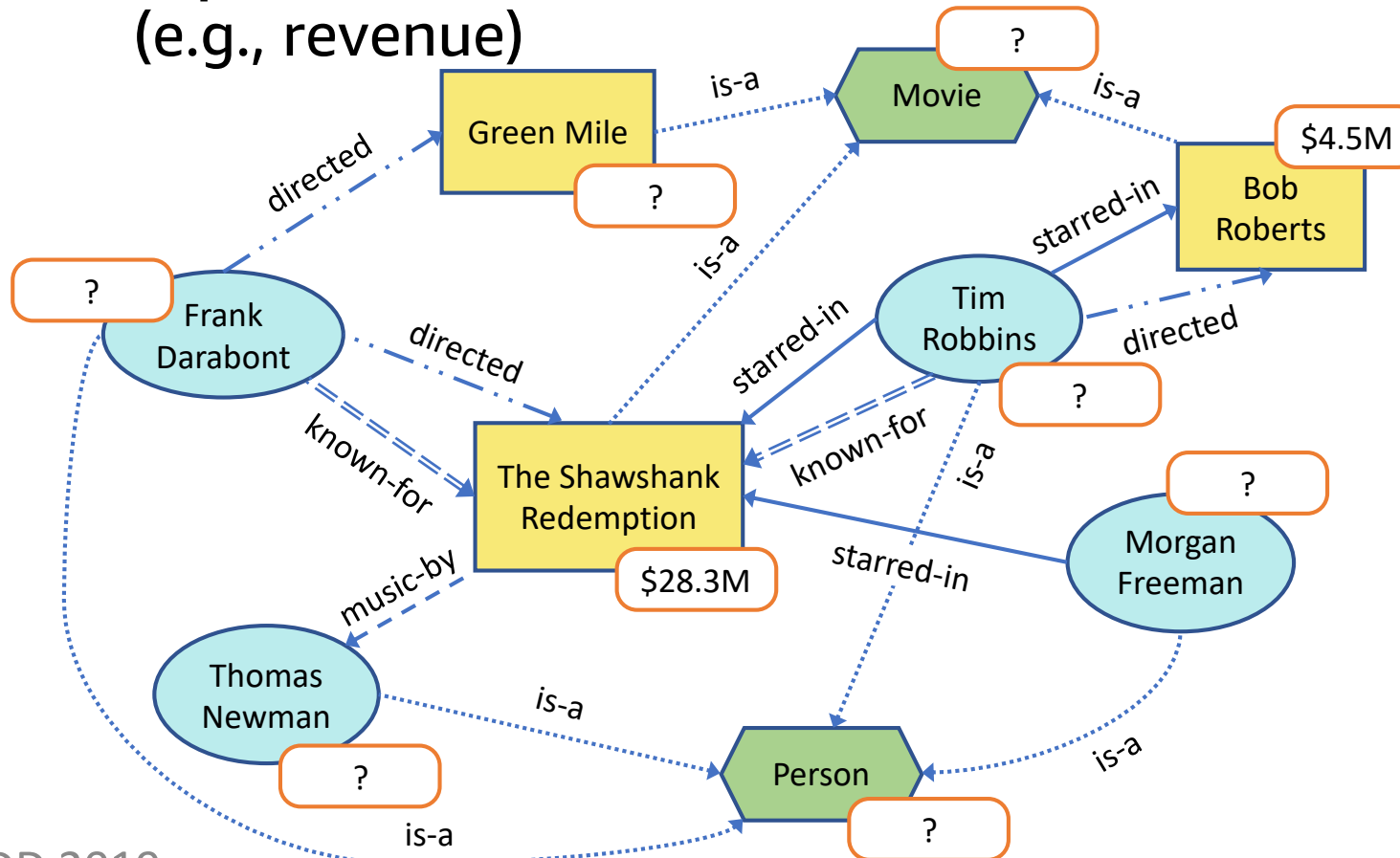
Input

- A knowledge graph
- Input scores for some nodes (e.g., revenue)



Output

- An importance score for each node
- Non-negative real value
 - Reflects the popularity of a node
 - Closely reconstructs input scores

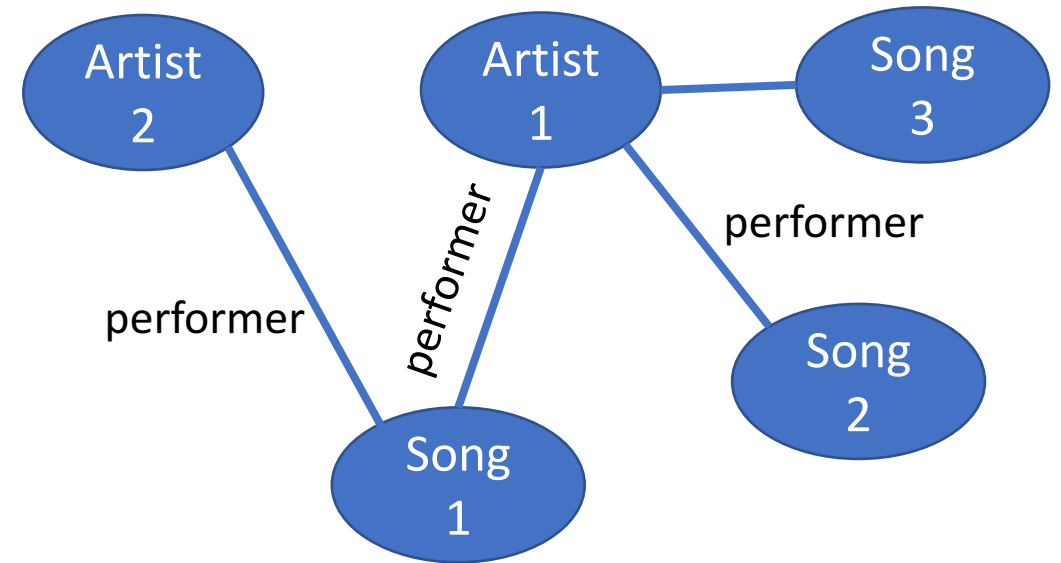


Node Importance Estimation: Intuition

- Which artist is more important?
 - Artist 1? Artist 2?

Requirements

Neighborhood Awareness



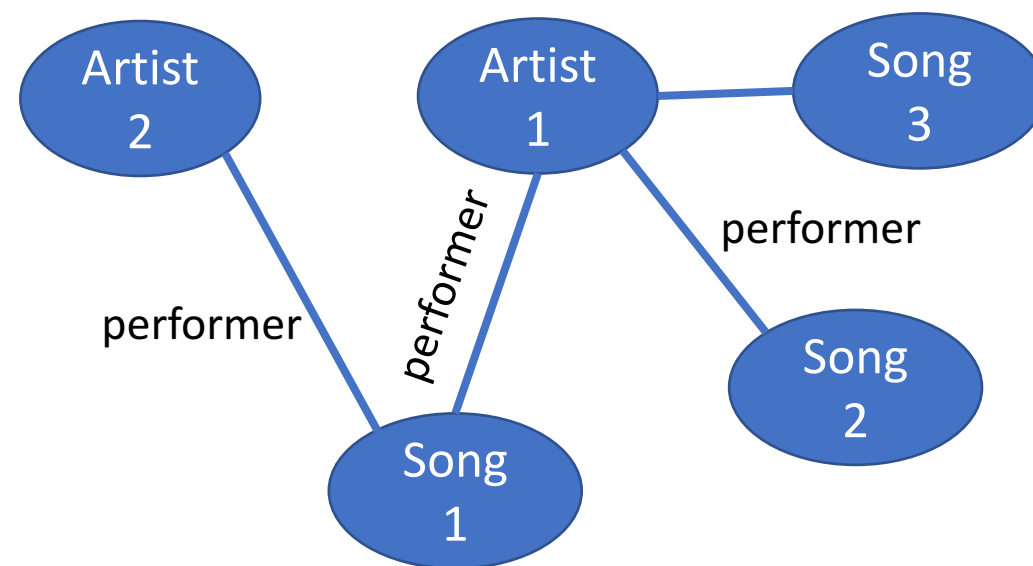
Node Importance Estimation: Intuition

- Which artist is more important?
 - Artist 1? Artist 2?

Requirements

Neighborhood Awareness

Centrality Awareness



Node Importance Estimation: Intuition

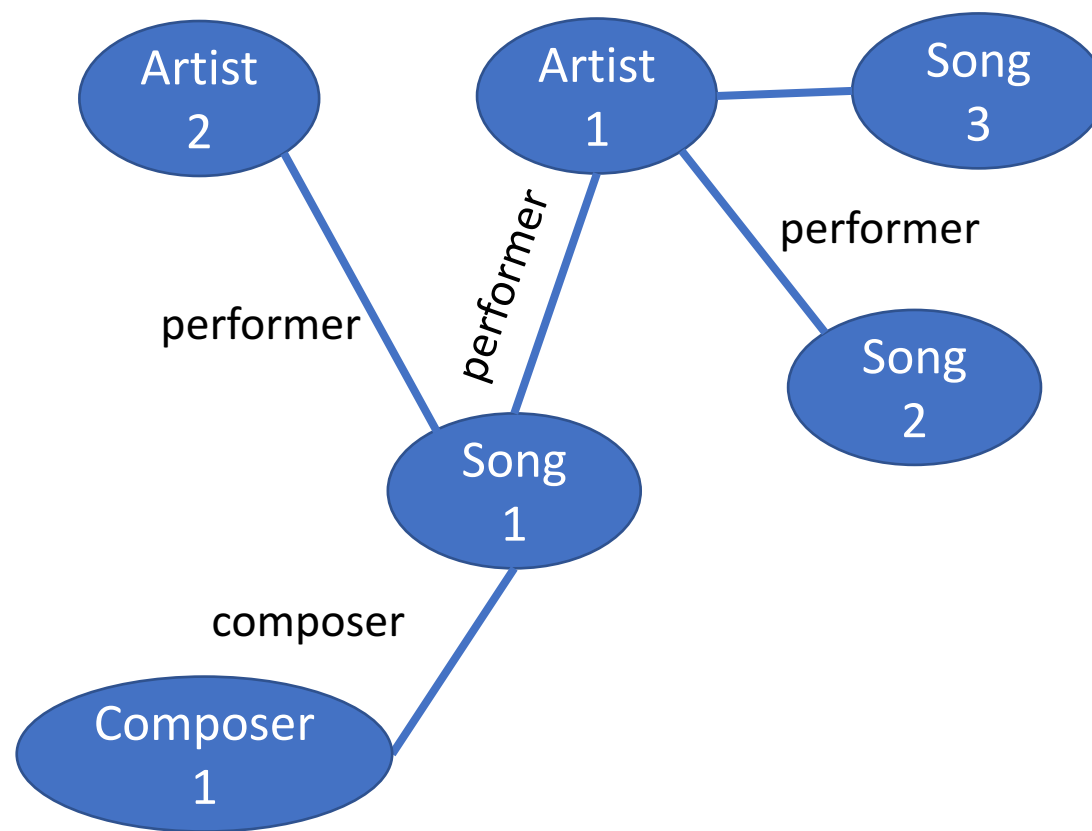
- What if there is a different predicate, e.g., a composer?

Requirements

Neighborhood Awareness

Centrality Awareness

Edge Type Awareness



Node Importance Estimation: Intuition

- We have access to importance scores for some nodes

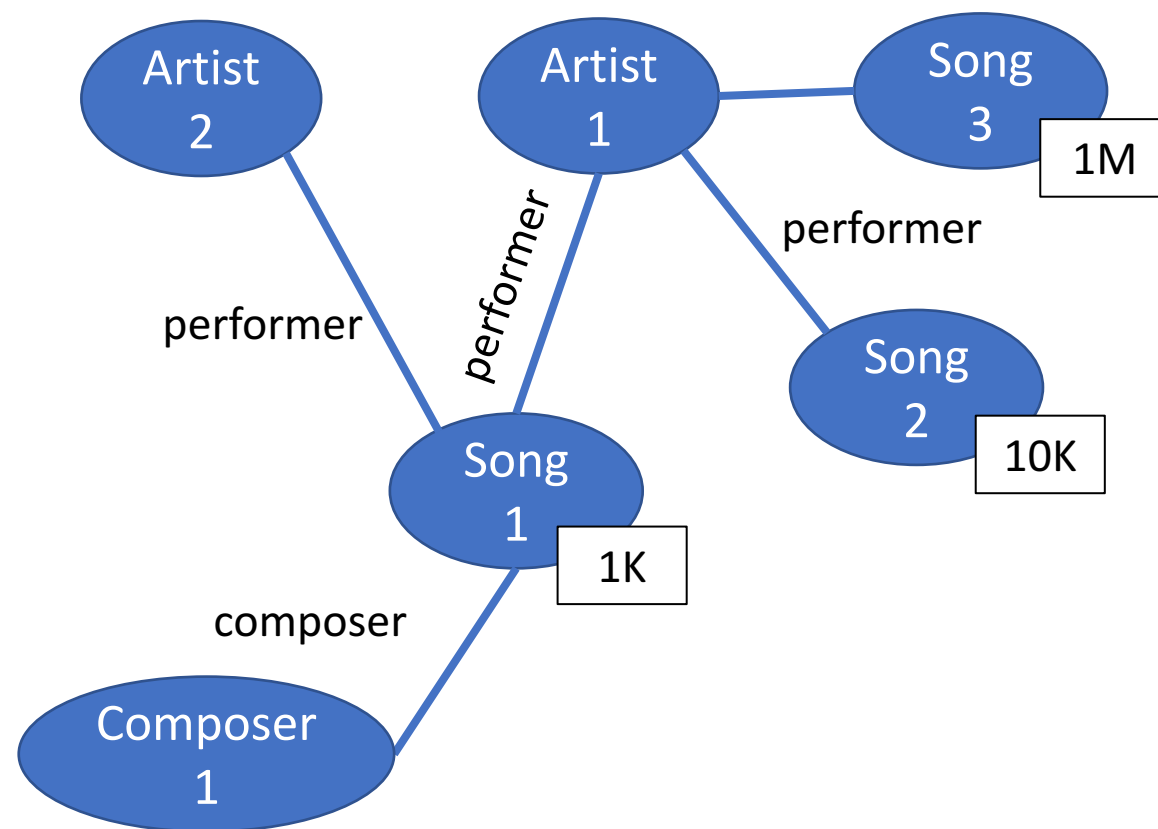
Requirements

Neighborhood Awareness

Centrality Awareness

Edge Type Awareness

Input Score Awareness



Node Importance Estimation: Intuition

- What if the score distribution changes?

Requirements

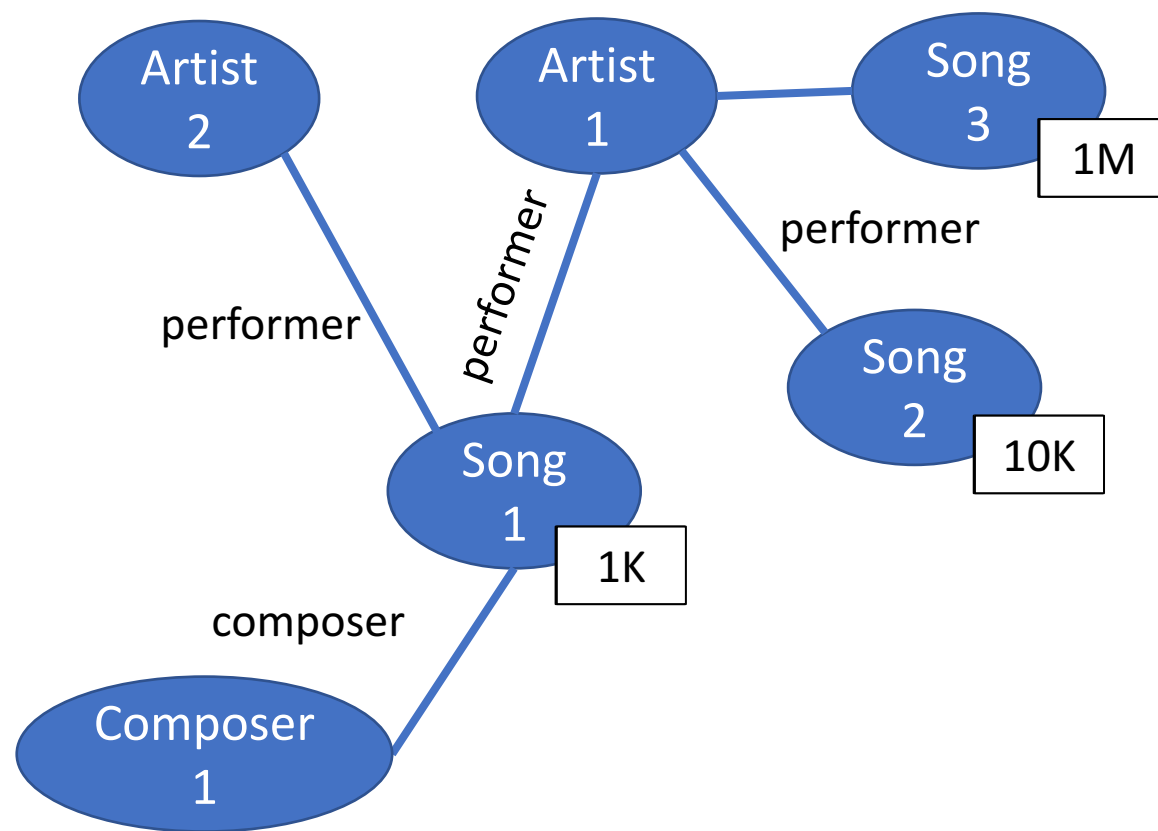
Neighborhood Awareness

Centrality Awareness

Edge Type Awareness

Input Score Awareness

Flexible Adaptation



Not a “Solved Problem”

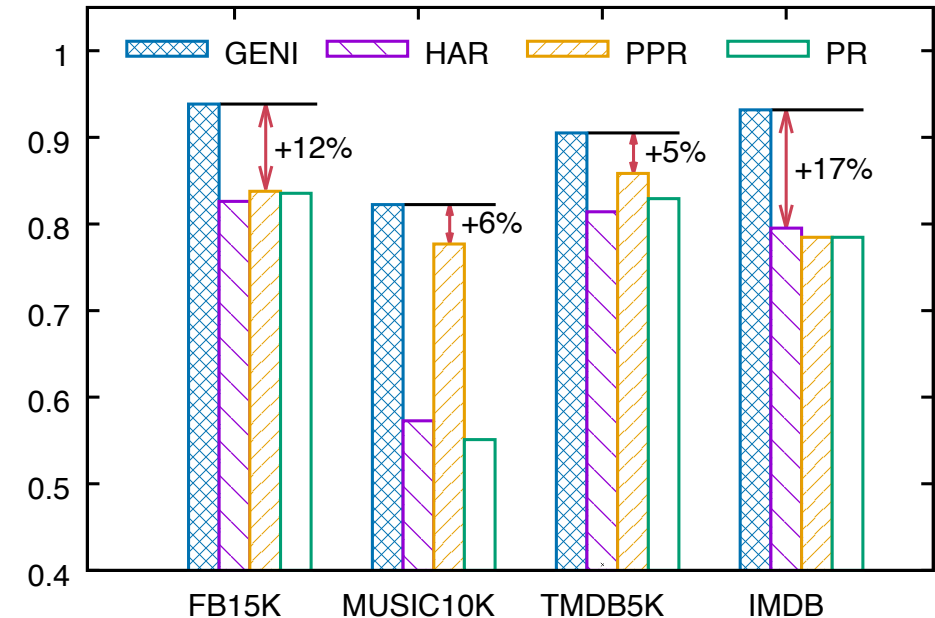
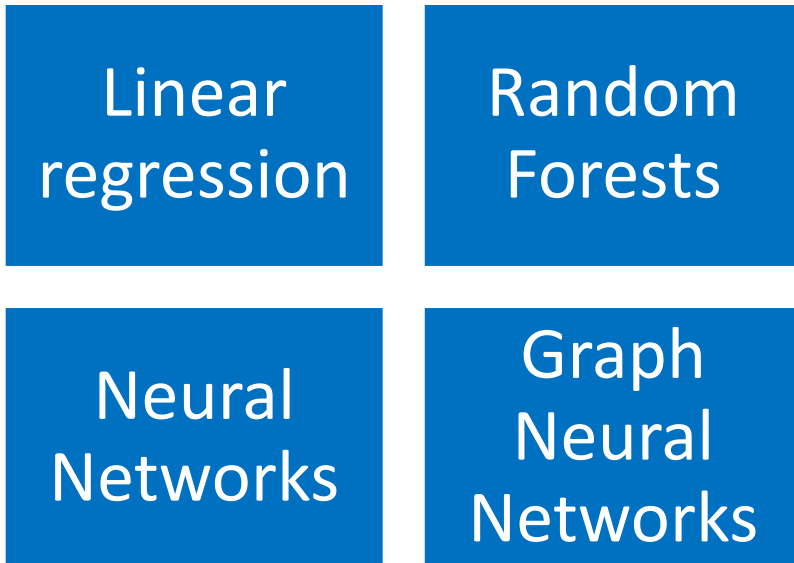
Requirements	PageRank	Personalized PageRank	HAR
Neighborhood Awareness	✓	✓	✓
Centrality Awareness	✓	✓	✓
Input Score Awareness		✓	✓
Edge Type Awareness			✓
Flexible Adaptation			

Our Contributions

We explore supervised machine learning algorithms for this task

We present GENI, a GNN-based method

We provide empirical evidence and analysis of GENI on real-world KGs



Roadmap

- Introduction
- **Proposed Method: GENI**
 - Main Ideas
 - Model Architecture
- Experimental Results
- Conclusion



Proposed Method: GENI

- We propose GENI, a **G**raph neural network (GNN) for **E**stimating **N**ode **I**mportance in a KG

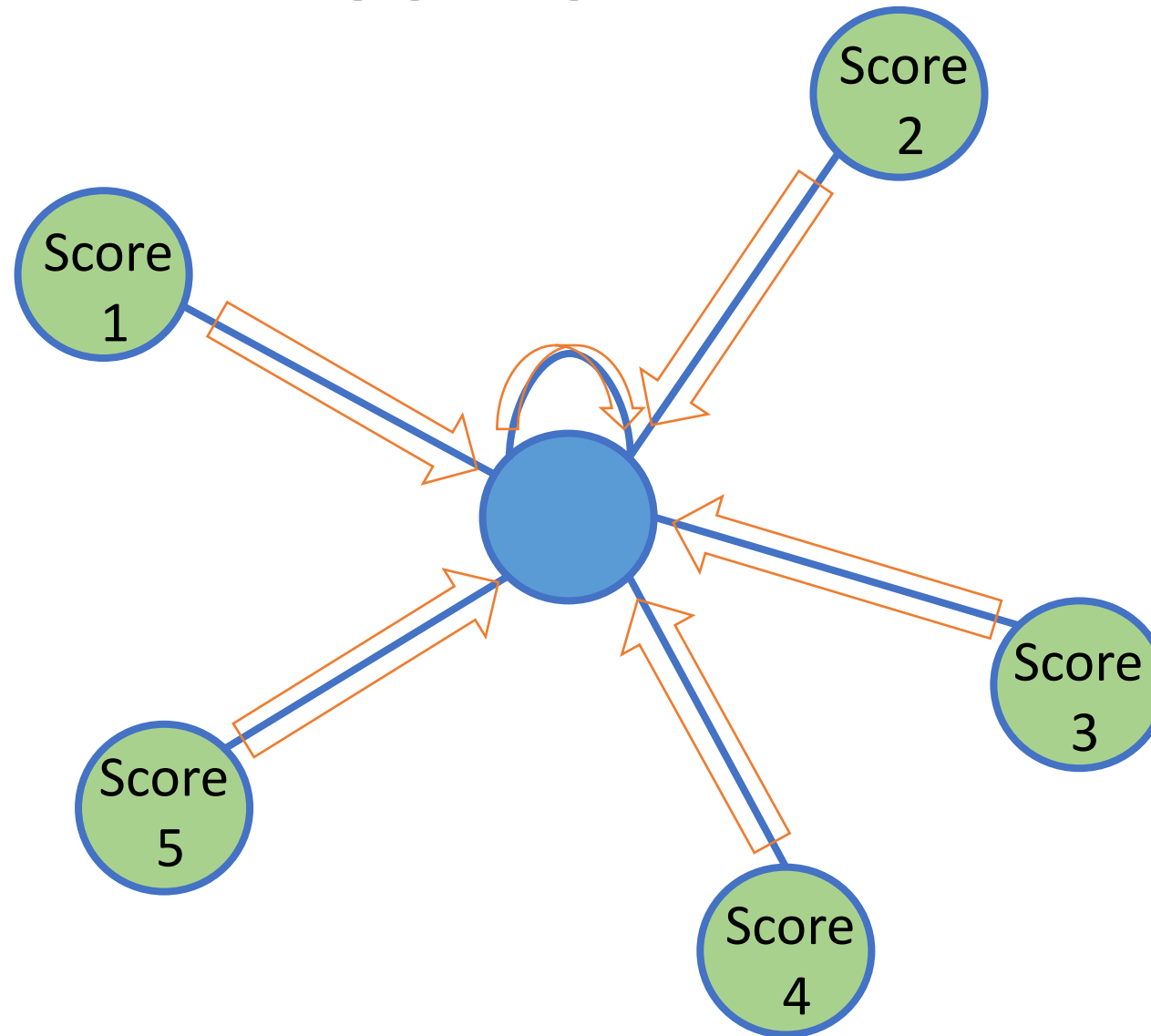
Requirements	PageRank	Personalized PageRank	HAR	GENI
Neighborhood Awareness	✓	✓	✓	✓
Centrality Awareness	✓	✓	✓	✓
Input Score Awareness		✓	✓	✓
Edge Type Awareness			✓	✓
Flexible Adaptation				✓

Proposed Method: GENI

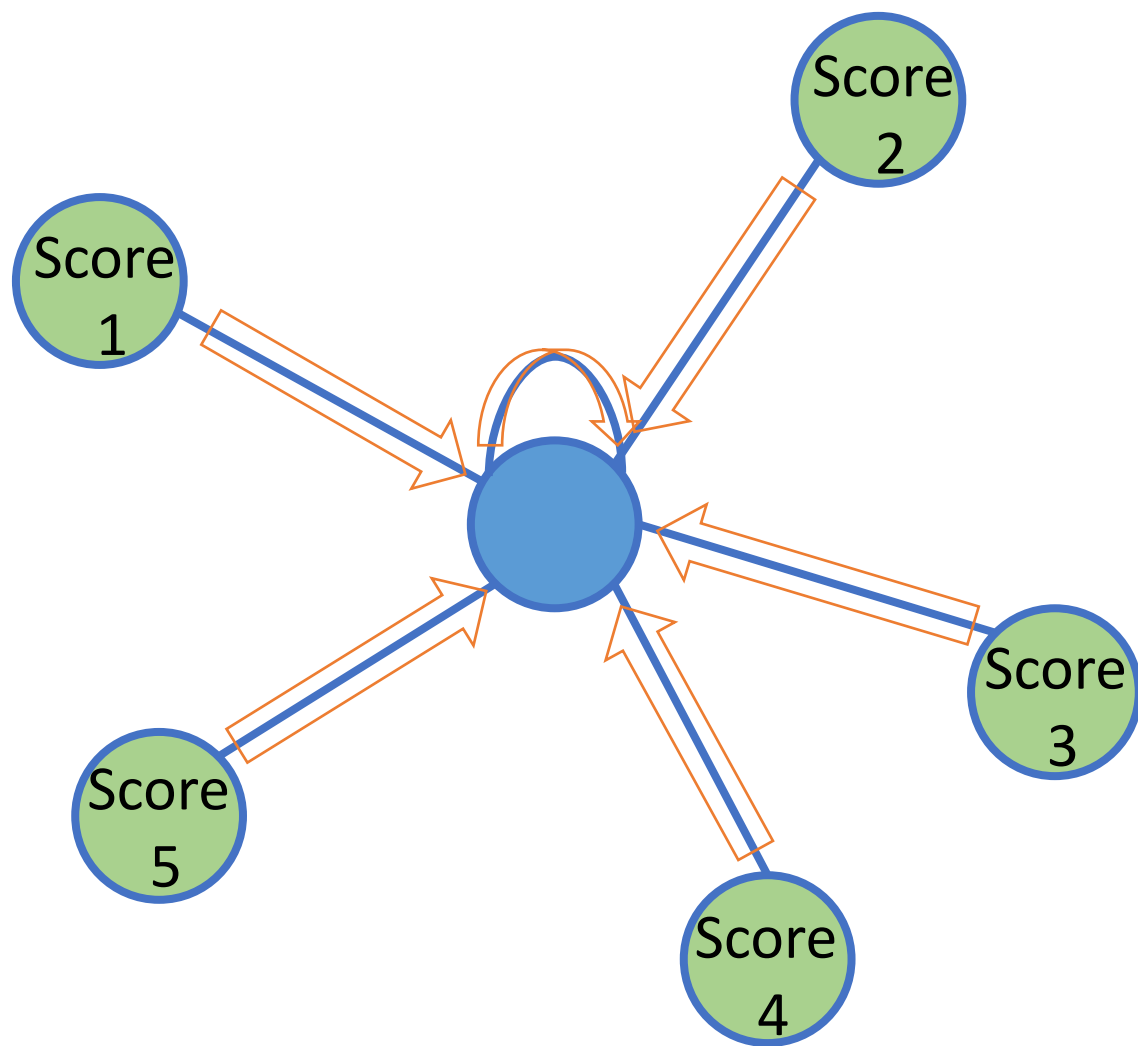
- We propose GENI, a **G**raph neural network (GNN) for **E**stimating **N**ode **I**mportance in a KG

Requirements	Our Solution
Neighborhood Awareness	Score Aggregation
Edge Type Awareness	Predicate-Aware Attention
Centrality Awareness	Centrality Adjustment
Input Score Awareness	Supervised GNN framework
Flexible Adaptation	

Idea 1: Score Aggregation



Idea 1: Score Aggregation

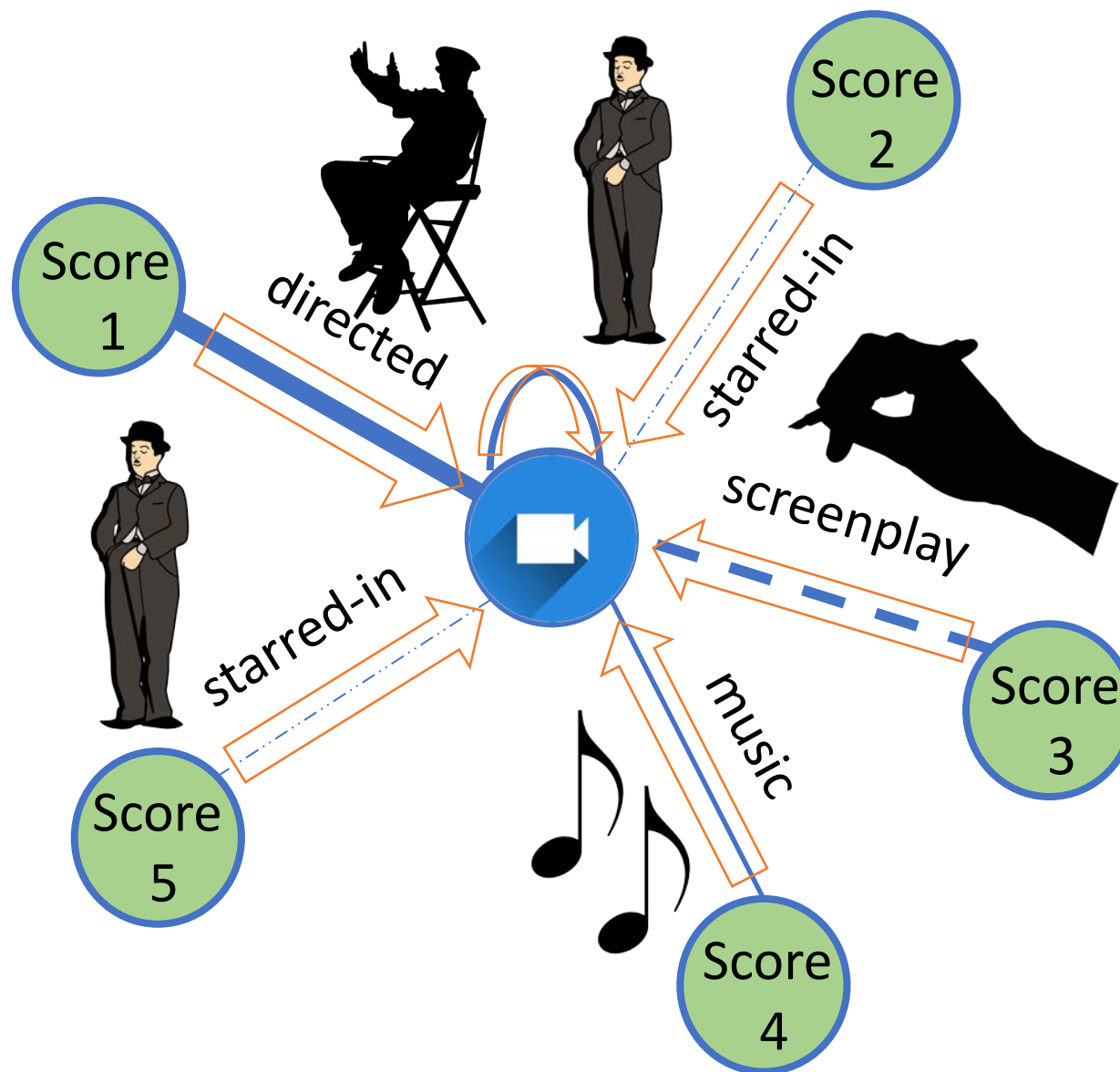


Score of a neighbor

$$s^{\ell}(i) = \sigma_s \left(\sum_{j \in \mathcal{N}(i) \cup \{i\}} \alpha_{ij}^{\ell} s^{\ell-1}(j) \right)$$

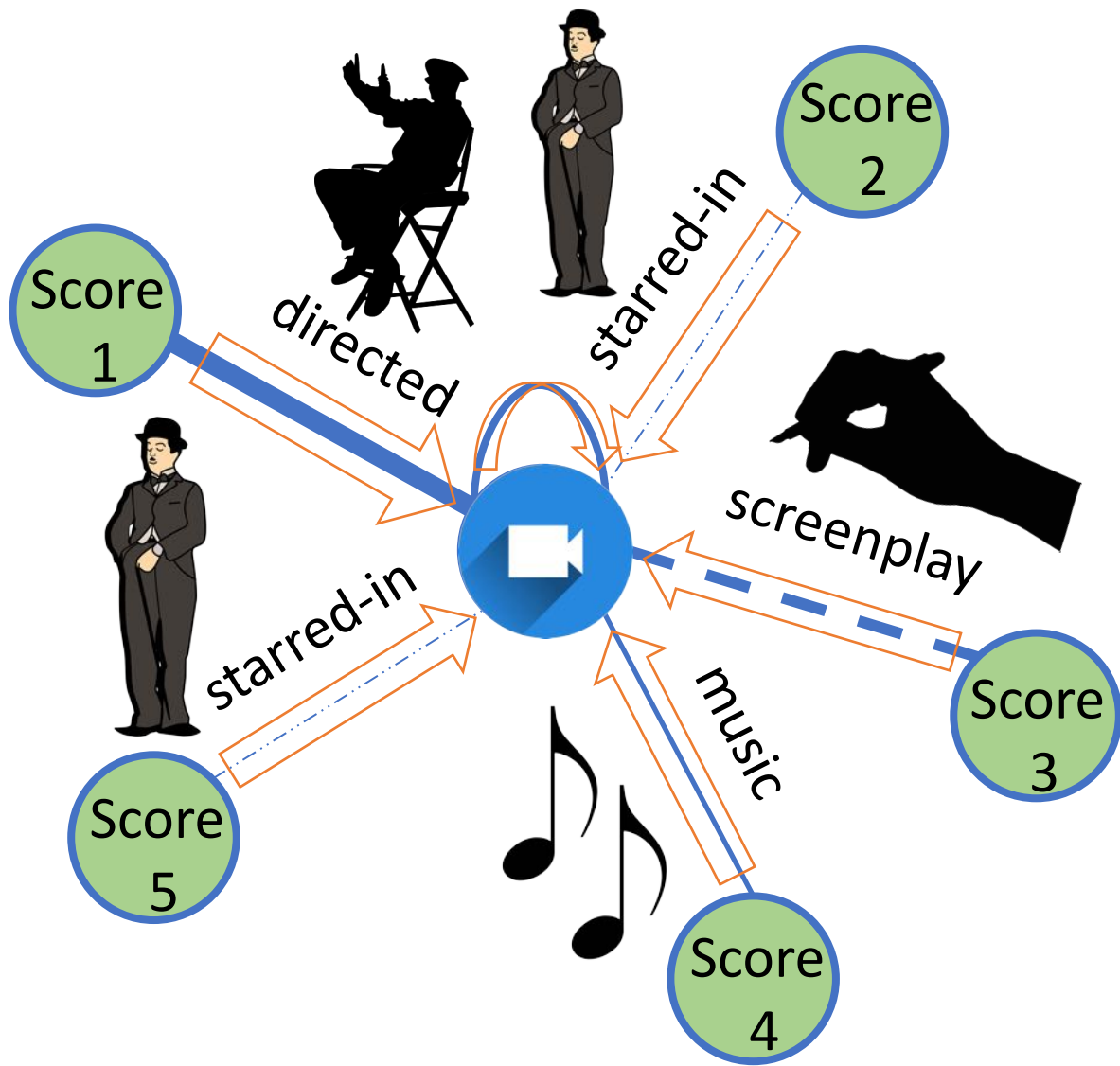
- ℓ : layer number
- $s^{\ell}(i)$: estimated score of node i
- $\mathcal{N}(i)$: neighbors of node i
- α_{ij}^{ℓ} : node i 's attention on node j

Idea 2: Predicate-Aware Attention



Idea 2: Predicate-Aware Attention

Detail



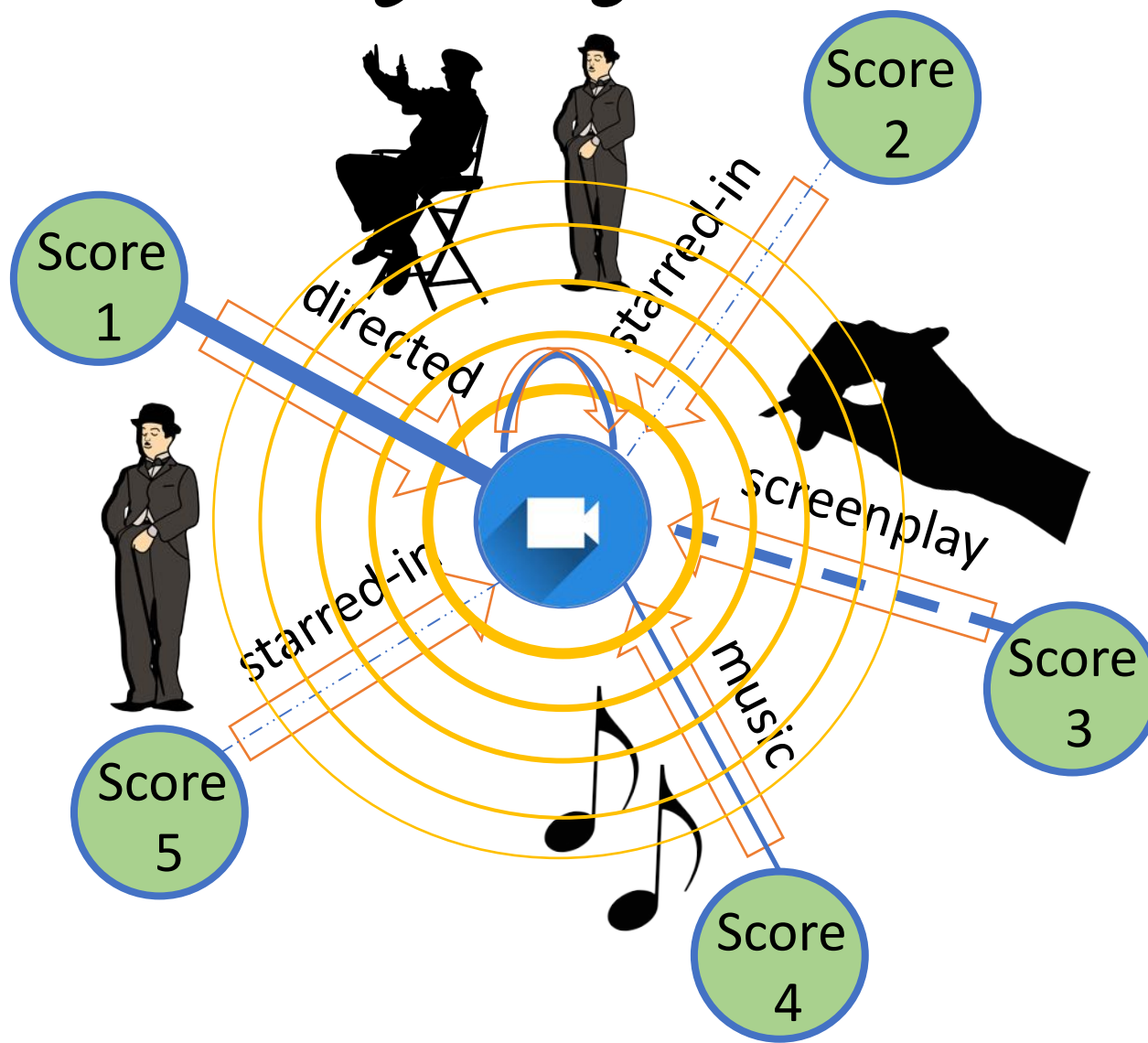
Attention considers predicate

$$s^\ell(i) = \sigma_s \left(\sum_{j \in \mathcal{N}(i) \cup \{i\}} \alpha_{ij}^\ell s^{\ell-1}(j) \right)$$

$$\alpha_{ij}^\ell = f(s^{\ell-1}(i), s^{\ell-1}(j), \vec{a}_\ell, \vec{p}_{ij})$$

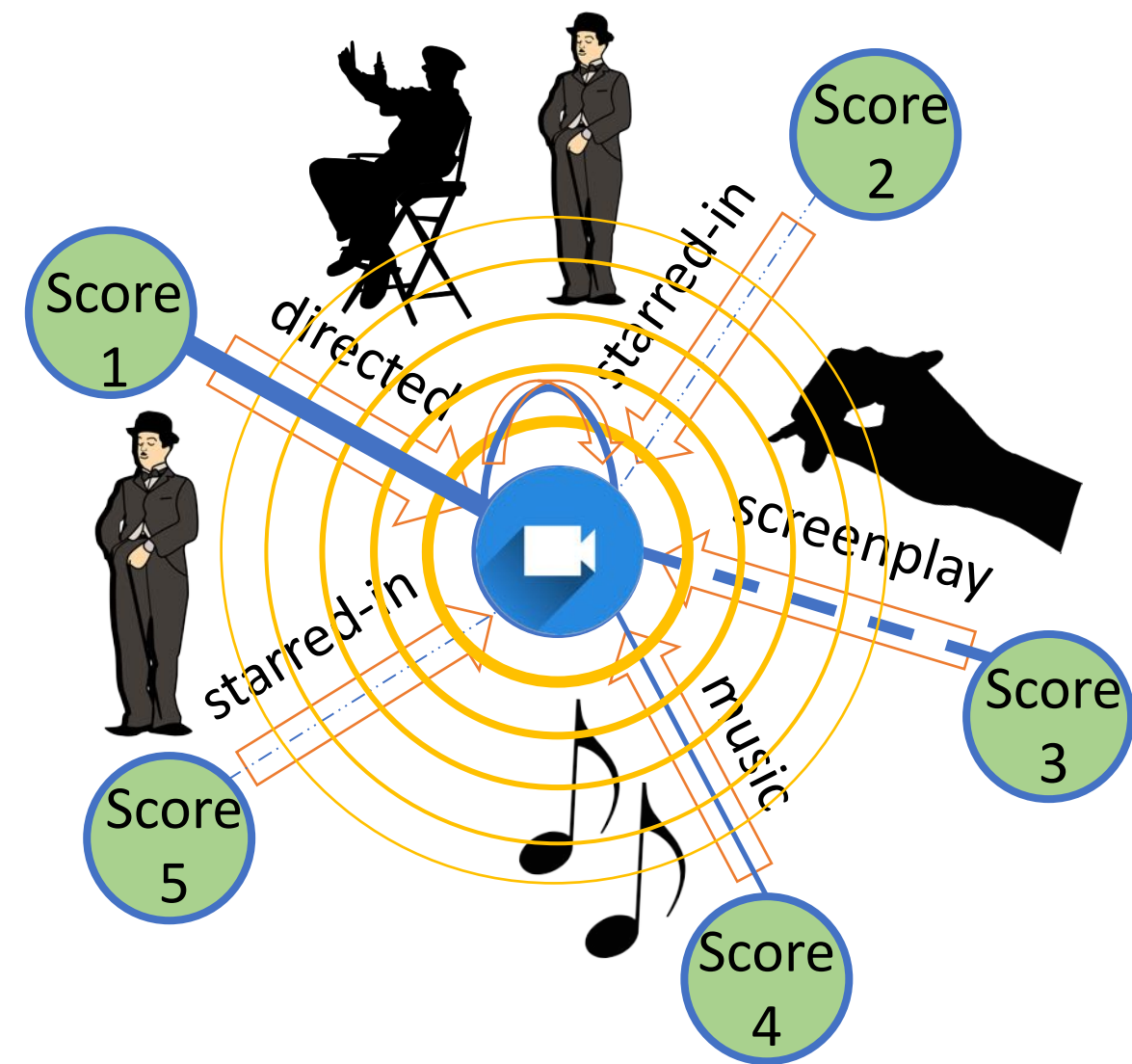
- α_{ij}^ℓ : node i 's attention on node j computed by the ℓ -th layer
- $s^\ell(i)$: estimated score of node i
- \vec{p}_{ij} : predicates of between nodes i and j
- \vec{a}_ℓ : attention parameters

Idea 3: Centrality Adjustment



Idea 3: Centrality Adjustment

Detail



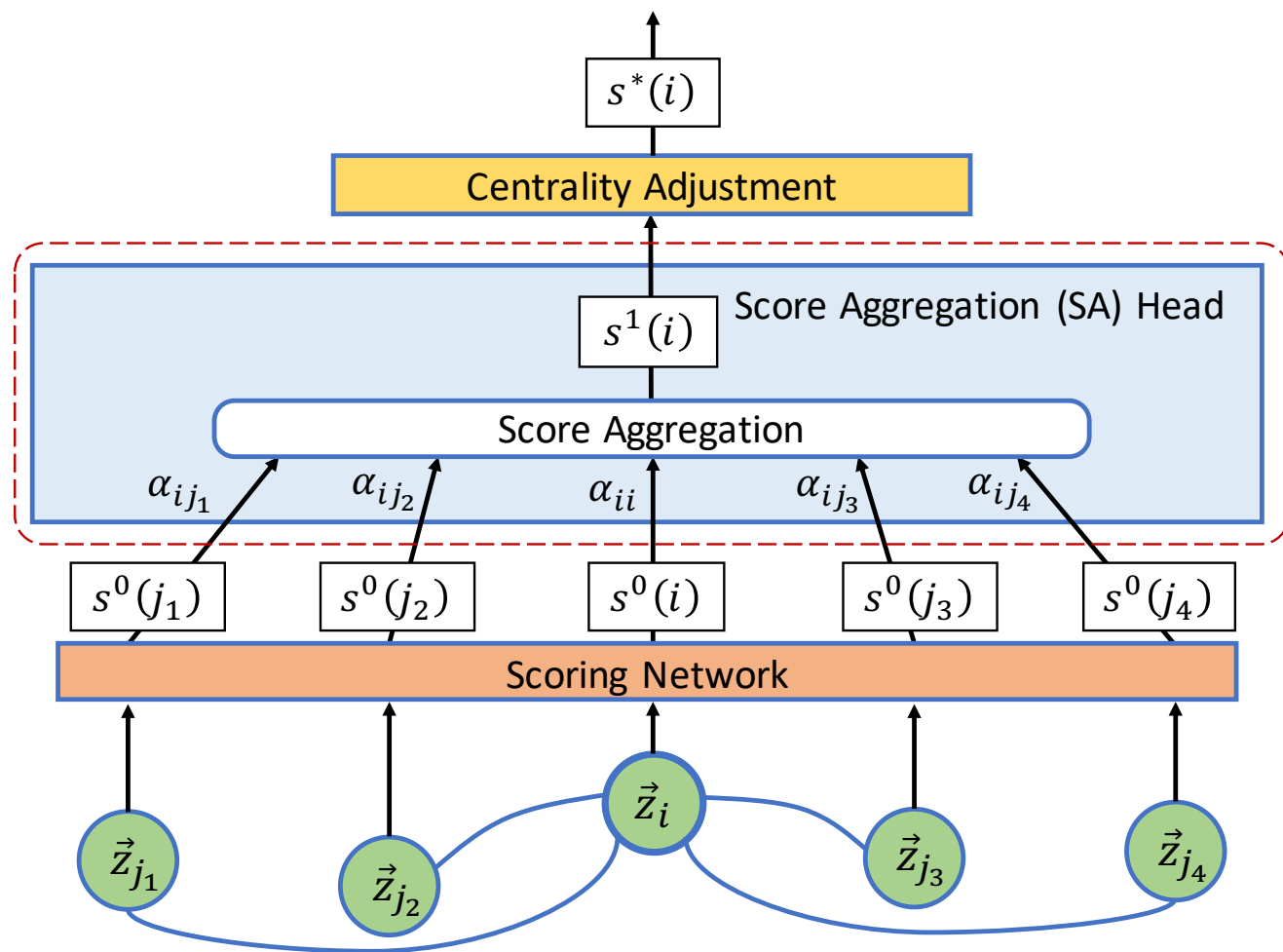
In-degree of a node

$$s^*(i) = \text{CentralityAdjustment}(s^L(i), d(i))$$

Estimated score before centrality adjustment

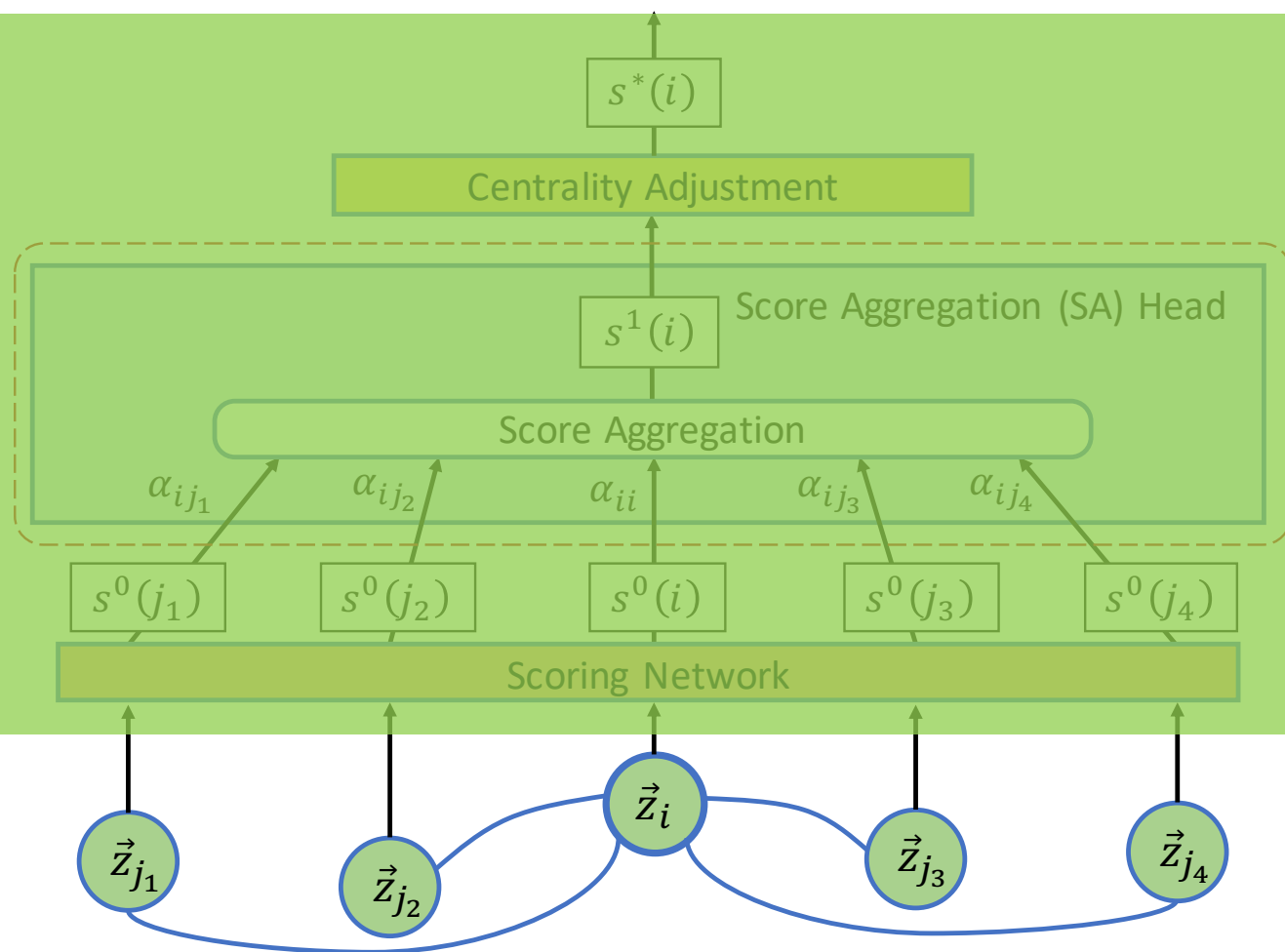
- $s^*(i)$: centrality-adjusted score estimation of node i
- $s^L(i)$: estimated score of node i before centrality adjustment
- $d(i)$: in-degree of node i
- L : final layer

Model Architecture: One Layer, One Head



- $s^*(i) = \text{Centr. Adj.}(s^1(i), d(i))$
- $s^1(i) = \text{ReLU}(\sum_{j \in \mathcal{N}(i) \cup \{i\}} \alpha_{ij}^1 s^0(j))$
- $\alpha_{ij}^1 = f(s^0(i), s^0(j), \vec{a}_1, \vec{p}_{ij})$
- $s^0(i) = \text{ScoringNetwork}(\vec{z}_i)$
- \vec{z}_i : feature vector of node i

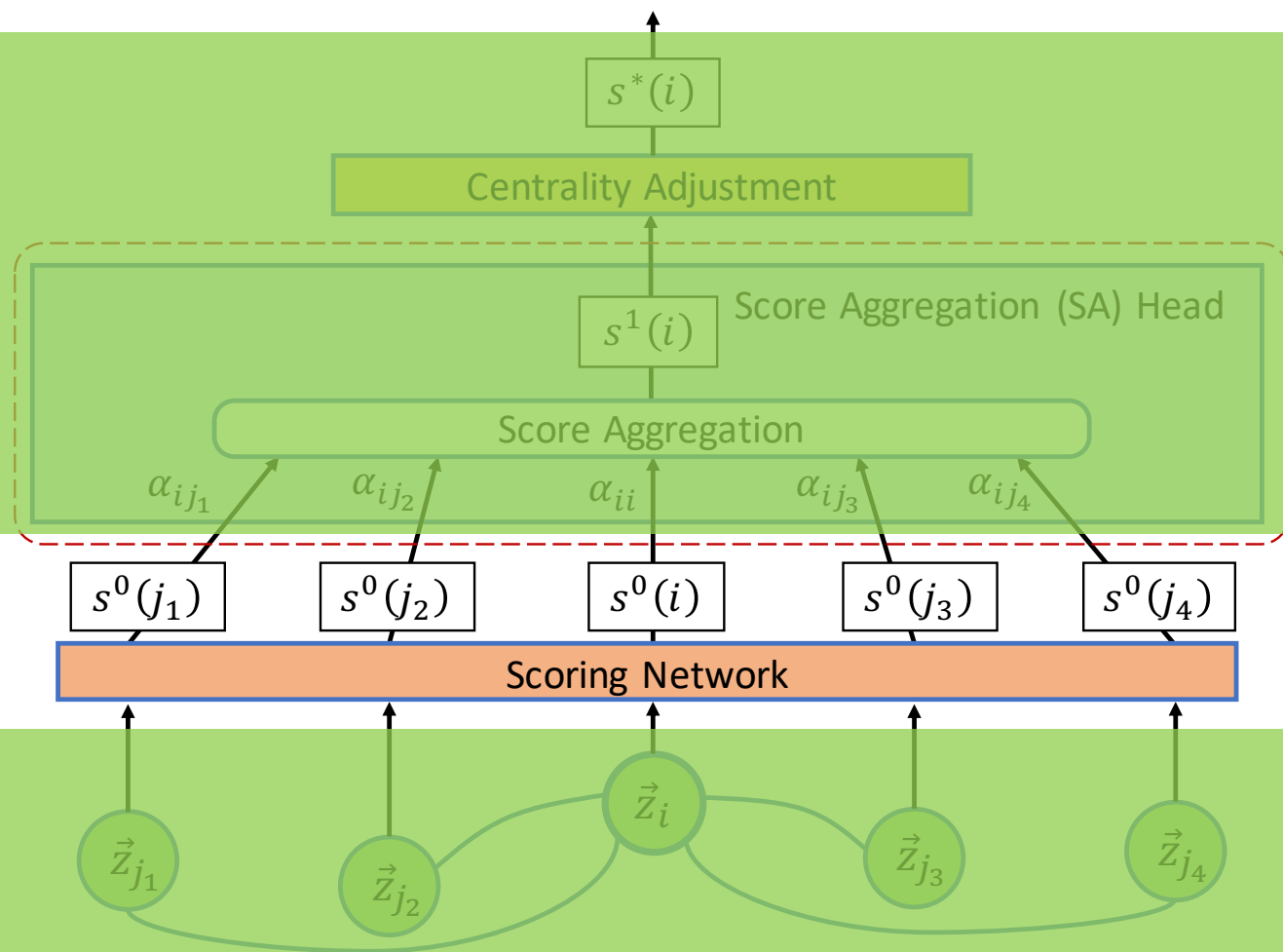
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- $s^0(i) = \text{ScoringNetwork}(\vec{z}_i)$

- \vec{z}_i : feature vector of node i
e.g., node2vec embeddings,
distributed bag-of-words
representation

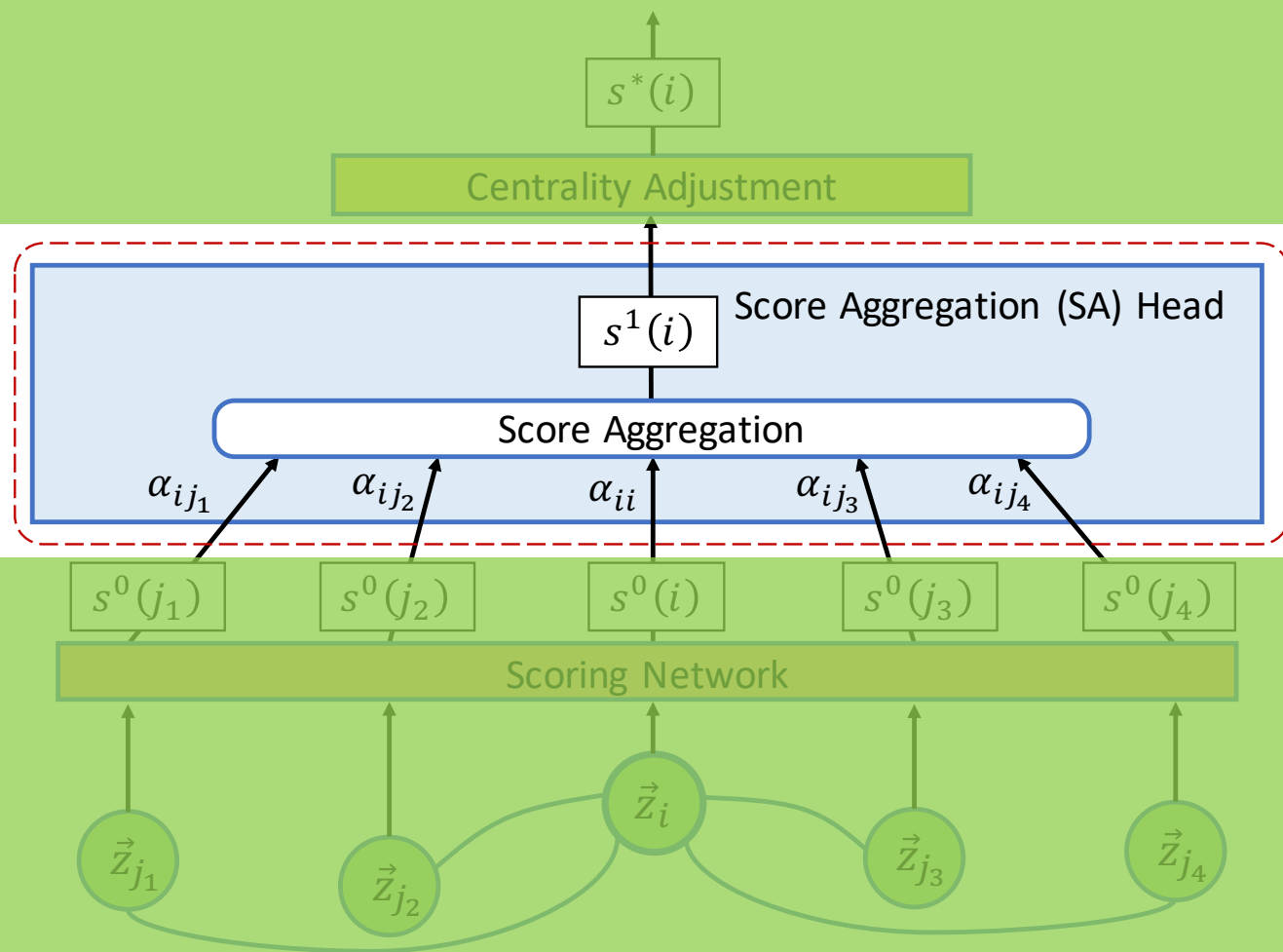
Model Architecture: One Layer, One Head



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Model Architecture: One Layer, One Head



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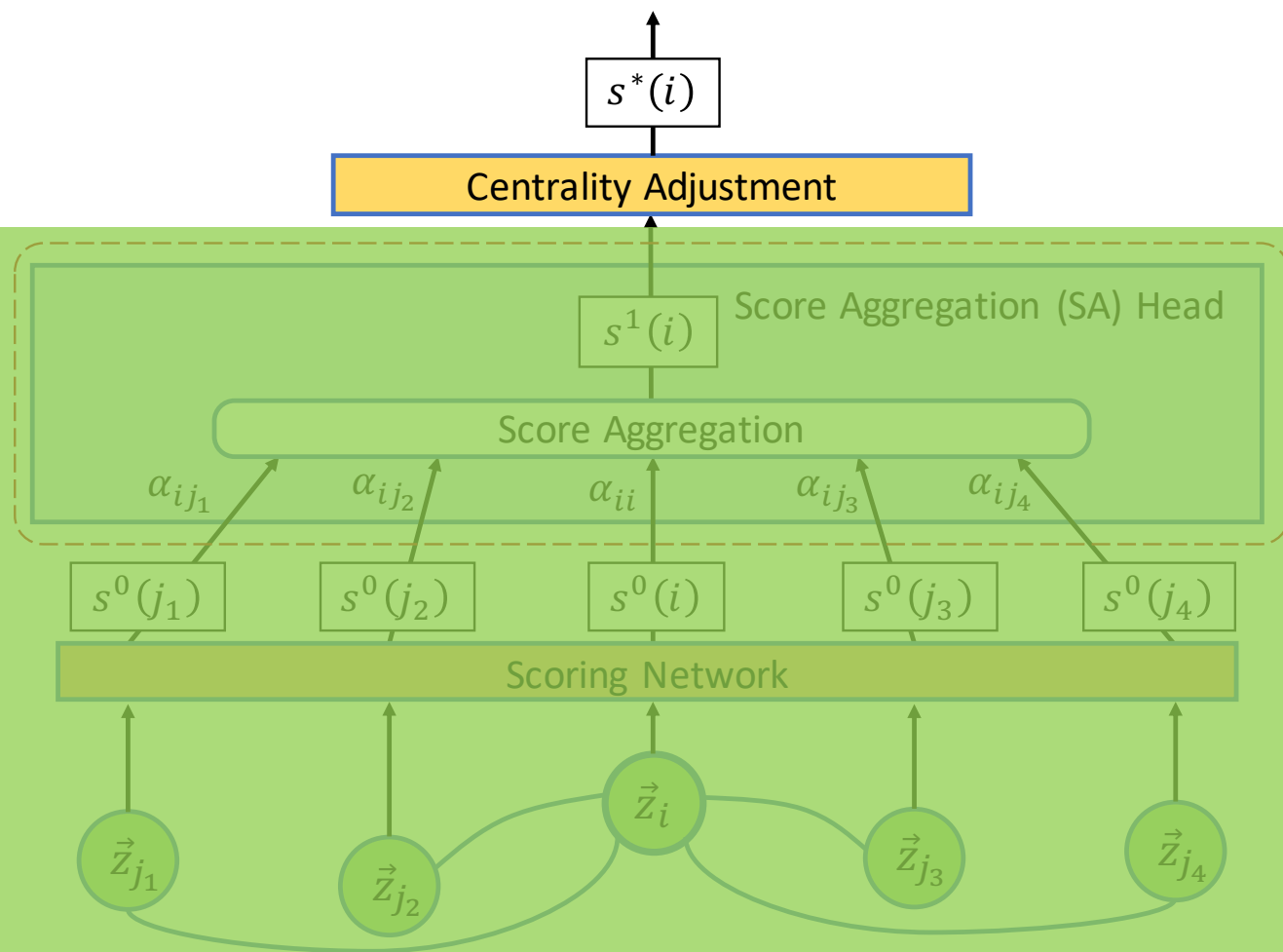
- $s^1(i) = \text{ReLU}(\sum_{j \in \mathcal{N}(i) \cup \{i\}} \alpha_{ij}^1 s^0(j))$

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Model Architecture: One Layer, One Head



- $s^*(i) = \text{Centr. Adj.}(s^1(i), d(i))$

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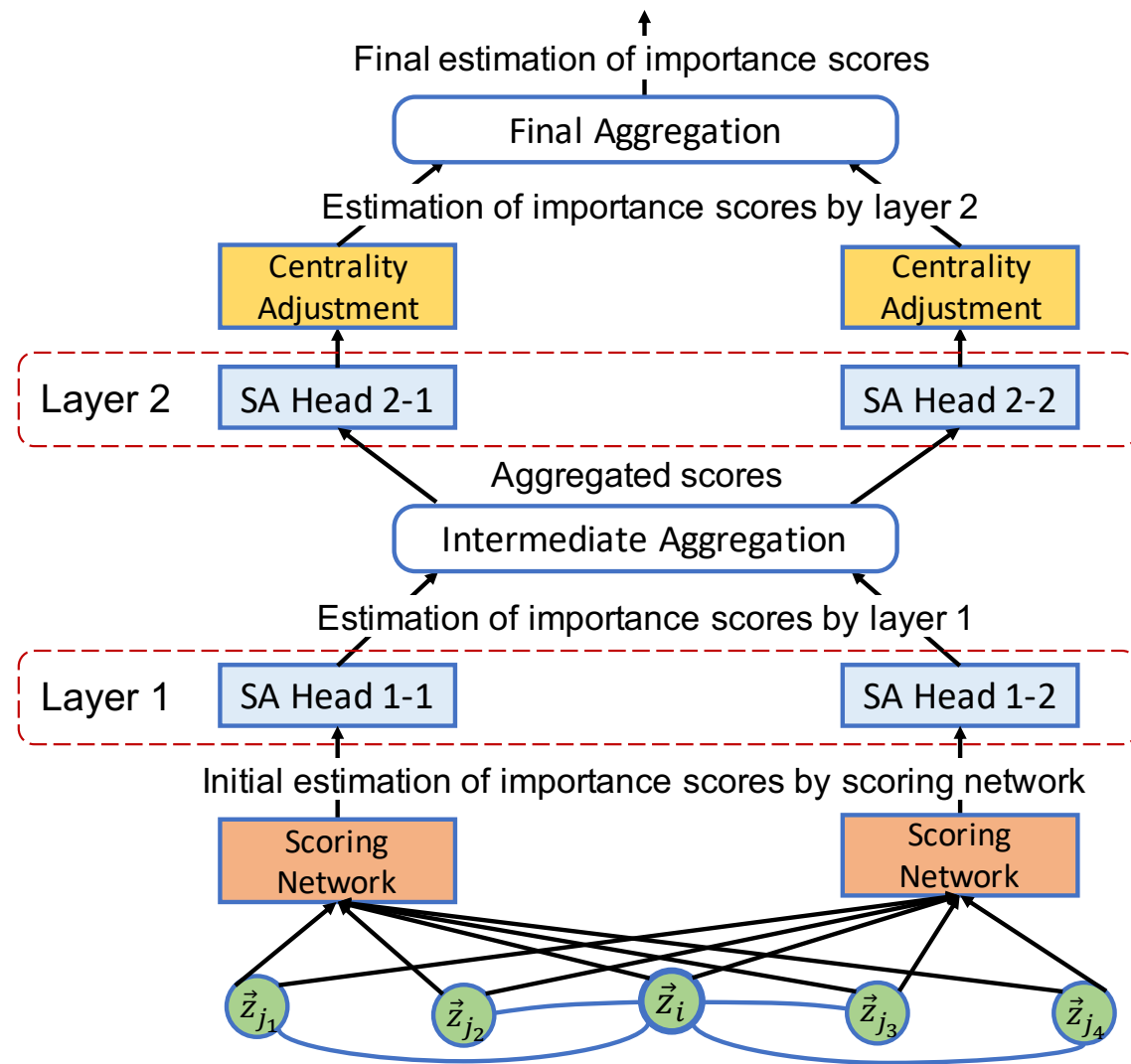
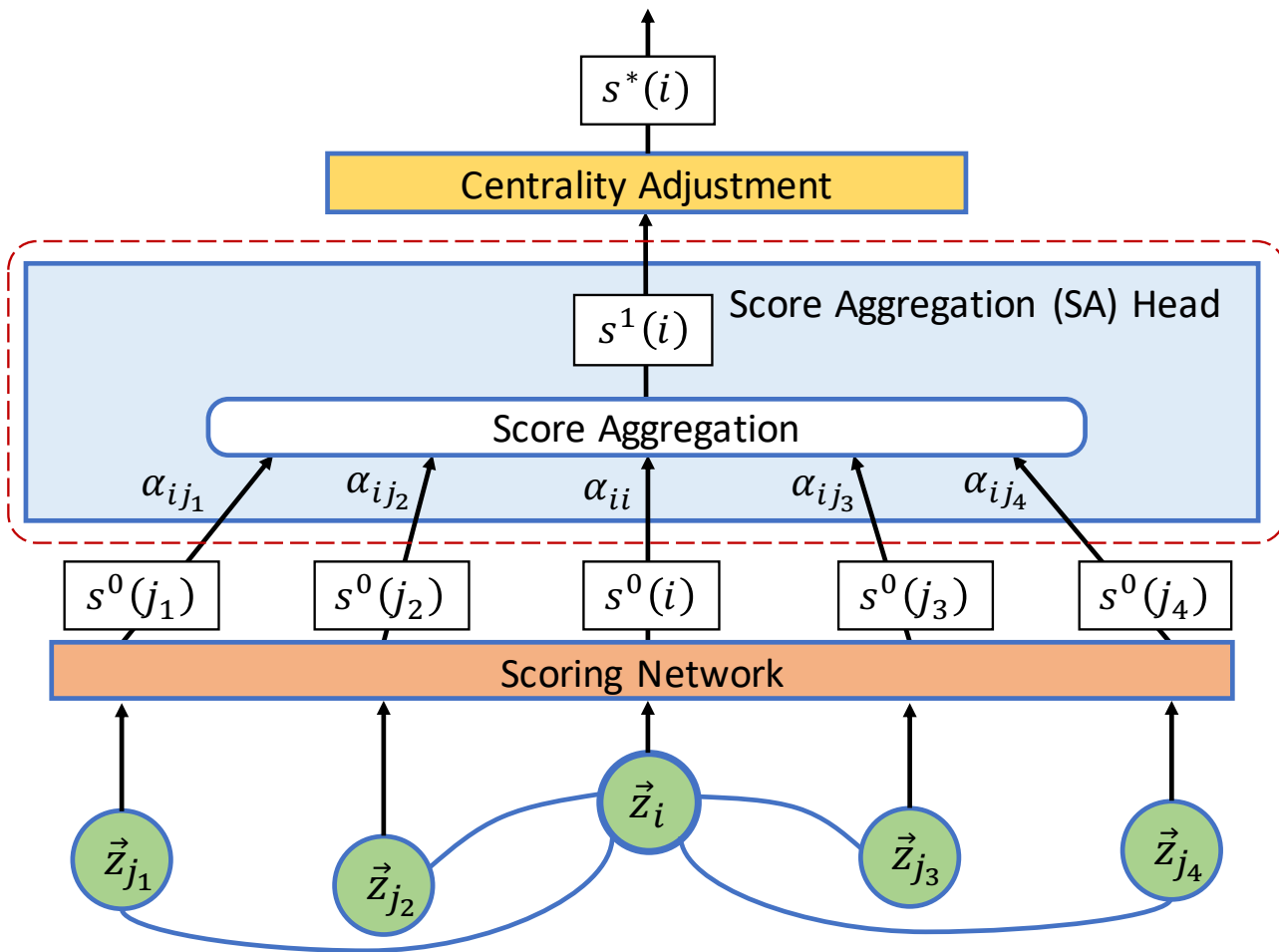
- $\alpha_{ij}^1 = f(s^0(i), s^0(j), \vec{a}_1, \vec{p}_{ij})$

- $s^0(i) = \text{ScoringNetwork}(\vec{z}_i)$

- \vec{z}_i : feature vector of node i
e.g., node2vec embeddings,
distributed bag-of-words
representation

Model Architecture: Multi Layer, Multi Head

Detail



Roadmap

- Introduction
- Proposed Method: GENI
- **Experimental Results**
- Conclusion



Experiments: Baselines

- Non-trainable approaches
 - PageRank (PR)
 - Personalized PageRank (PPR)
 - Hub, Authority, and Relevance score (HAR)
- Supervised approaches
 - Linear regression (LR)
 - Random forests (RF)
 - Neural networks (NN)
 - Graph attention networks (GAT)

Experiments: Datasets



Name	# Nodes	# Edges	# Predicates	Input Score Type	# Nodes w/ Scores
FB15K	14,951	592,213	1,345	# Pageviews	14,108 (94%)
MUSIC10K	24,830	71,846	10	Song hotttnesss	4,214 (17%)
TMDB5K	123,906	532,058	22	Movie popularity	4,803 (4%)
IMDB	1,567,045	14,067,776	28	# Votes for movies	215,769 (14%)

Experiments: Evaluation Strategies

We answer the following questions

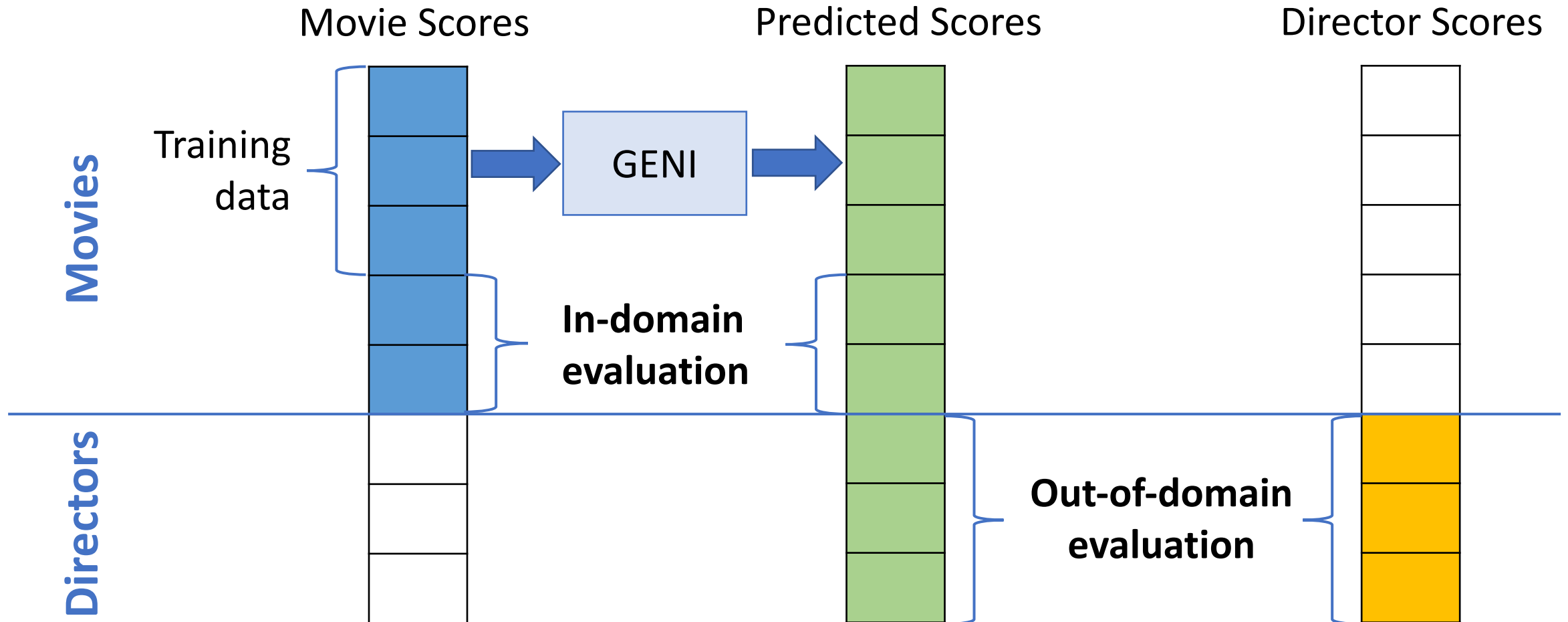
[Q1] How well does each method estimate node importance w.r.t. the given input score type?

→ “In-domain” evaluation

[Q2] How well does the estimation of each method generalize to the node of unseen types?

→ “Out-of-domain” evaluation

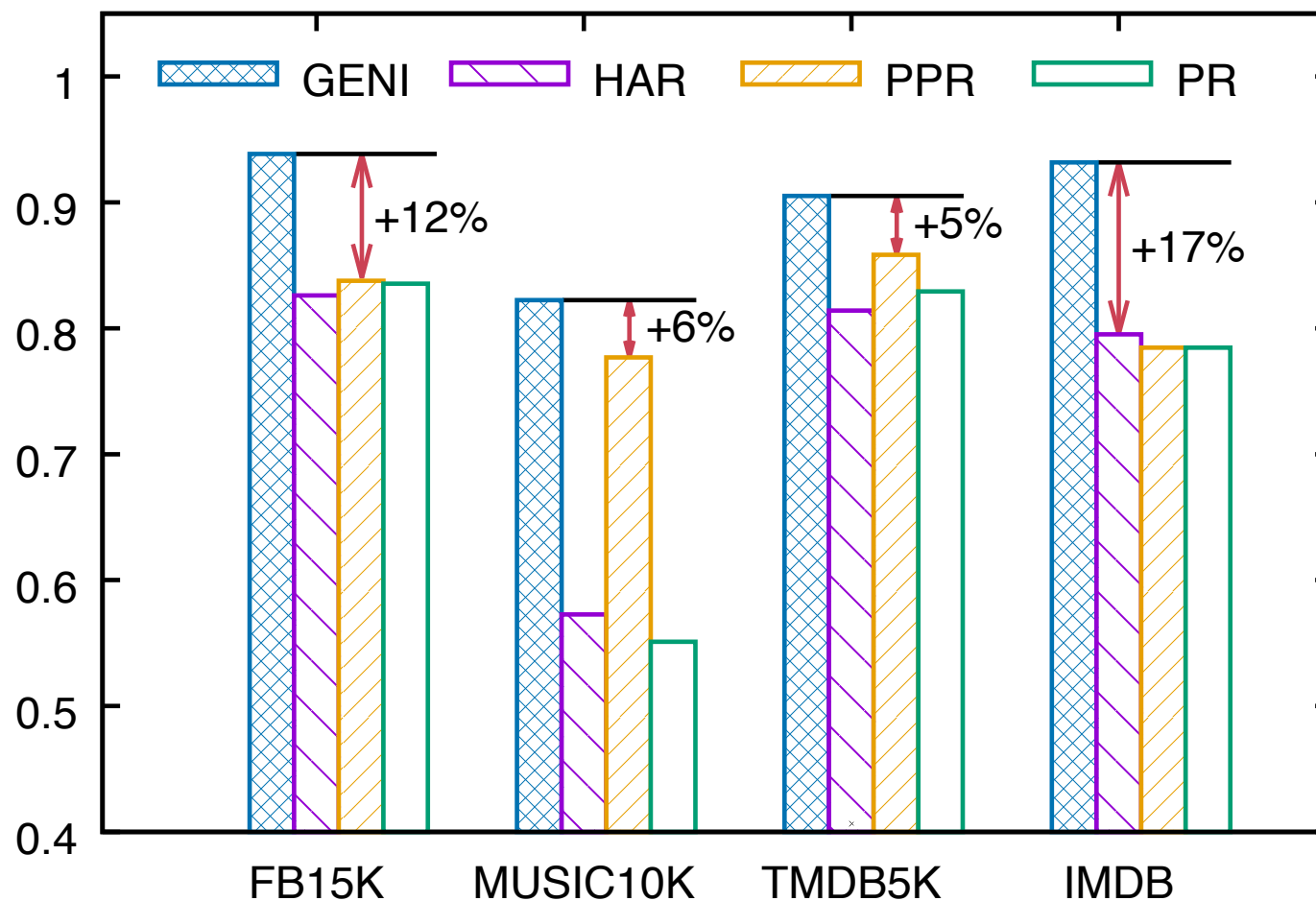
Experiments: Evaluation Strategies



In-Domain Evaluation

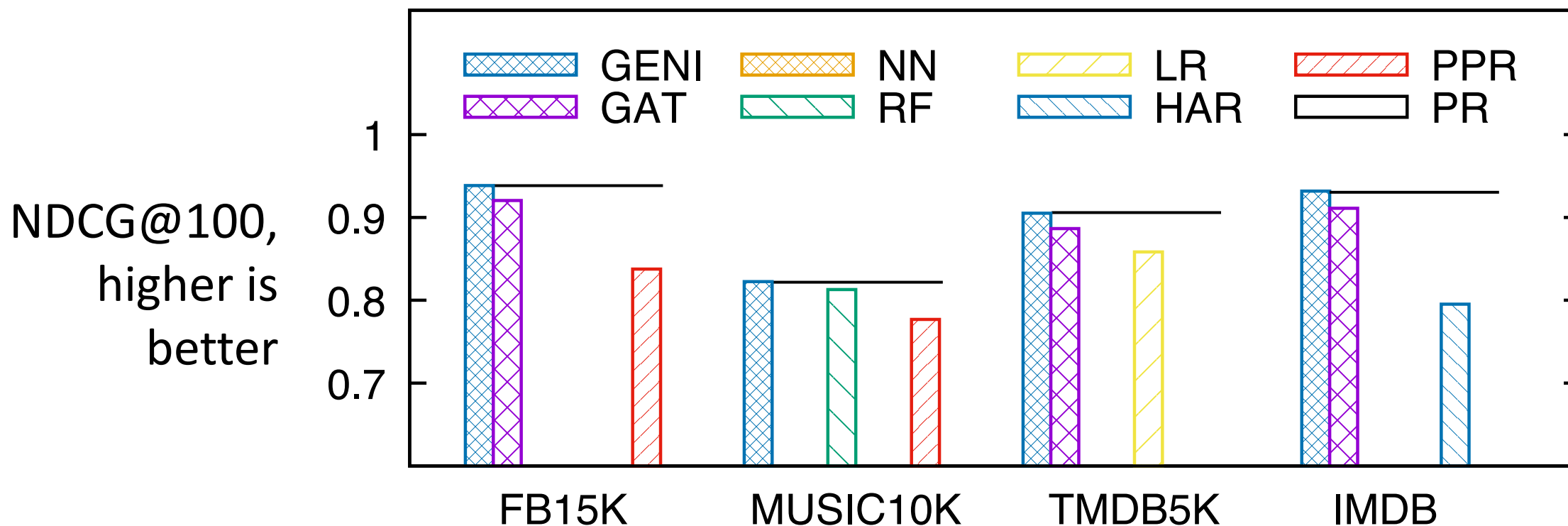
GENI (leftmost) outperforms baselines

NDCG@100,
higher is
better



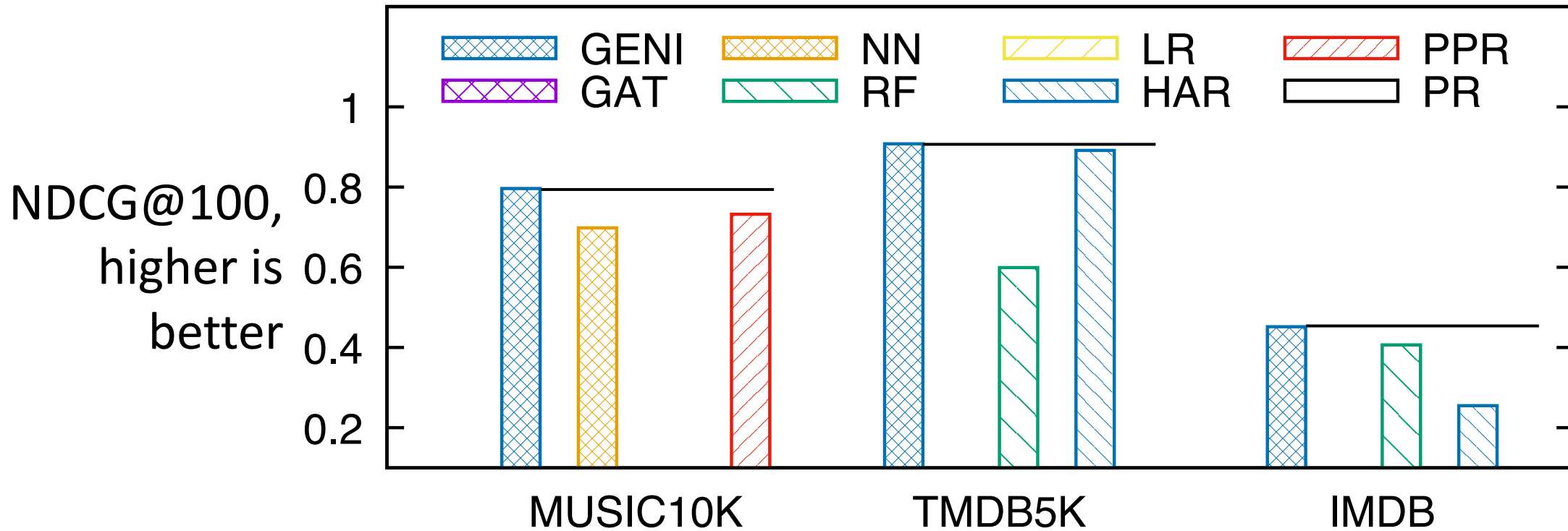
In-Domain Evaluation

GENI (leftmost) outperforms baselines



Out-Of-Domain Evaluation

GENI (leftmost) outperforms baselines



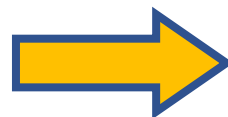
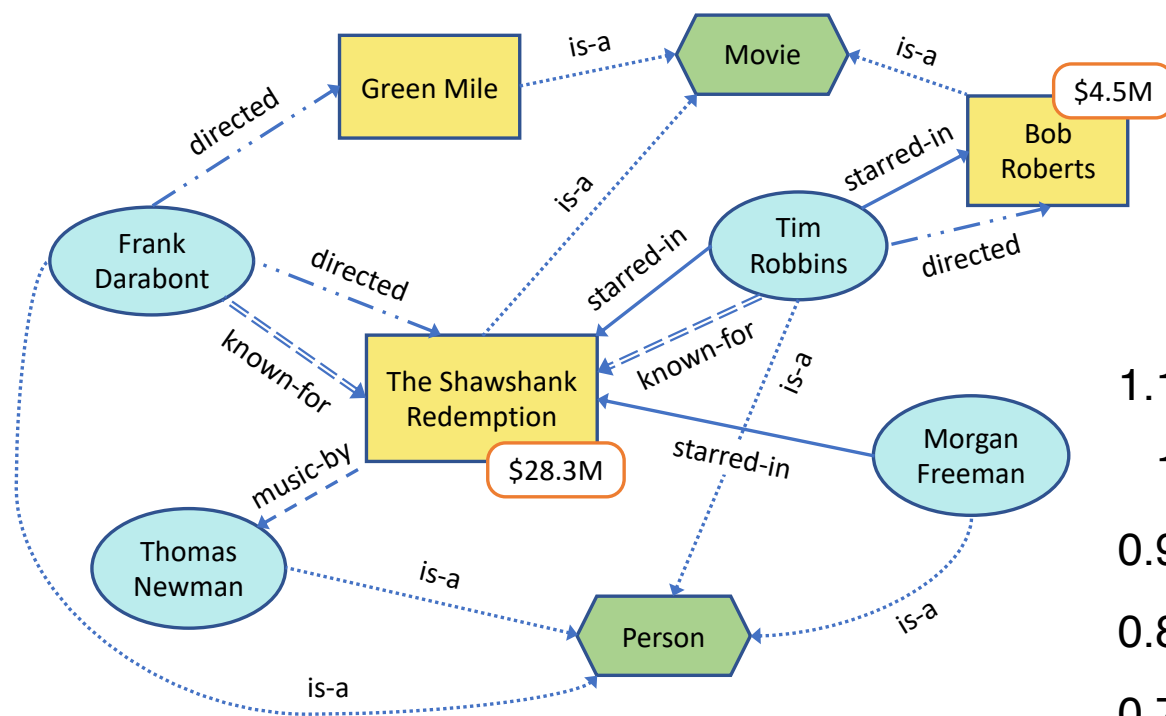
	MUSIC10K	TMDB5K	IMDB
Input Scores	Song hotttnesss	Movie popularity	# Votes for Movies
Out-Of-Domain Scores	Artist hotttnesss	Director ranking	Director ranking

Roadmap

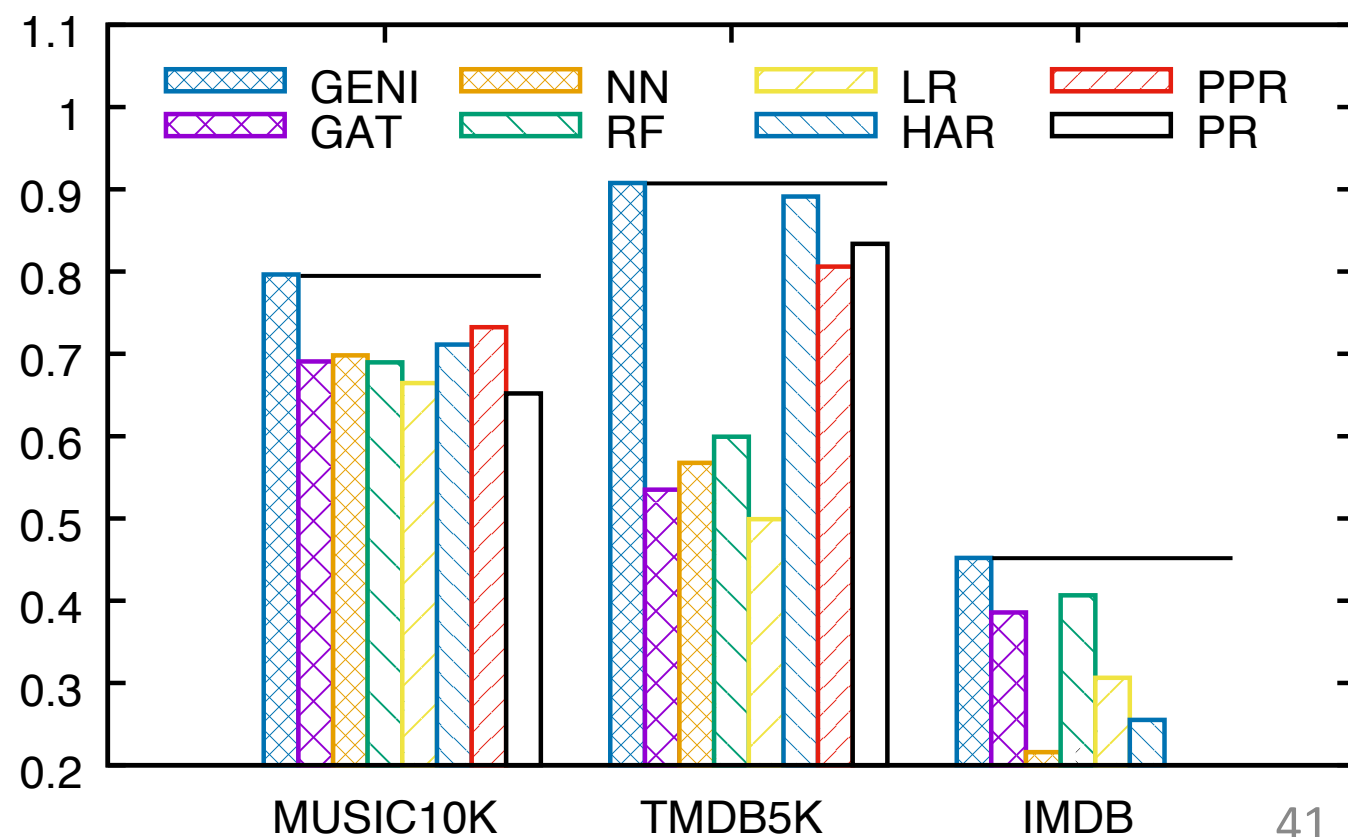
- Introduction
- Proposed Method: GENI
- Experimental Results
- **Conclusion**



Conclusion



- Our method GENI outperforms baselines in estimating node importance in a KG
- Future directions include considering multiple importance scores as input signals

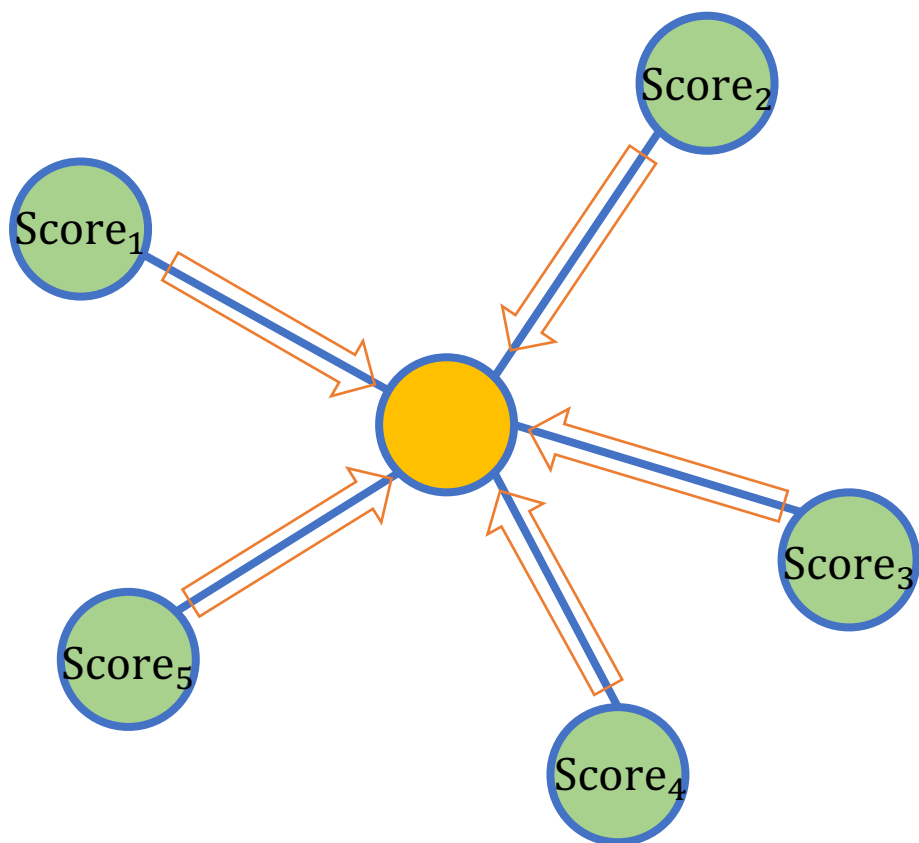


Thank you!

Appendix

Idea 1: Score Aggregation

- Initial scores $s^0(\cdot)$ are computed by ScoringNetwork, a feed forward NN trained jointly with the rest of GENI



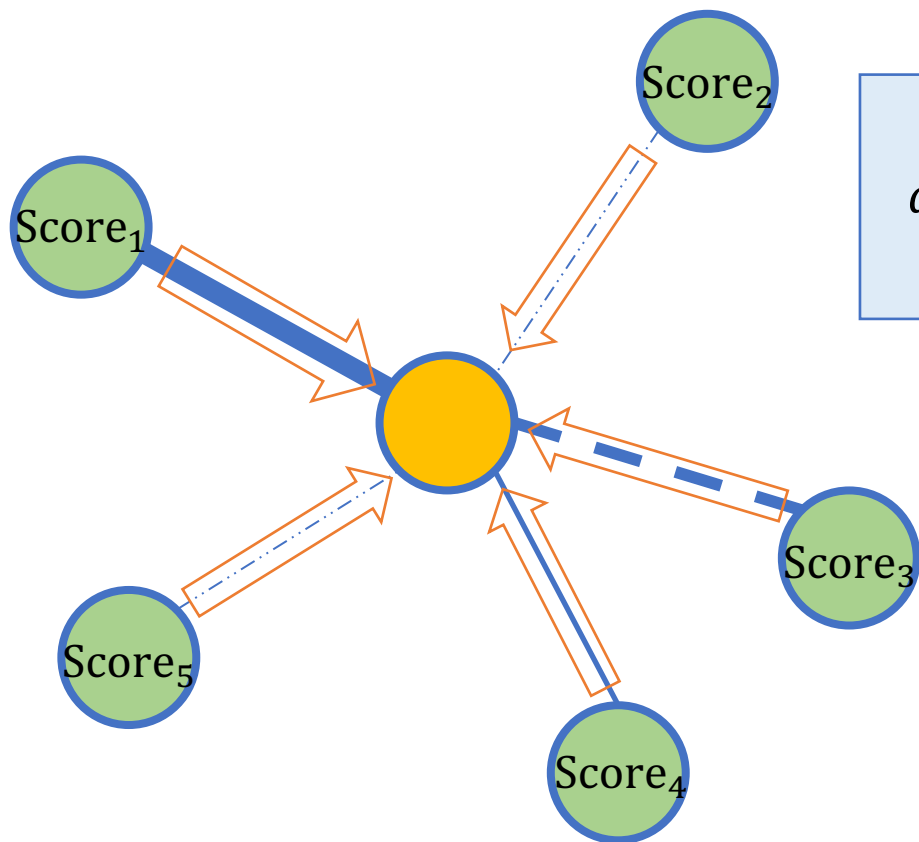
$$s^0(i) = \text{ScoringNetwork}(\vec{z}_i)$$

$$s^\ell(i) = \sigma_s \left(\sum_{j \in \mathcal{N}(i) \cup \{i\}} \alpha_{ij}^\ell s^{\ell-1}(j) \right)$$

- \vec{z}_i : feature vector of node i
- $s^0(i)$: initial score estimation of node i
- $s^\ell(i)$: estimated score of node i
- $\mathcal{N}(i)$: neighbors of node i
- α_{ij}^ℓ : node i 's attention on node j

Idea 2: Predicate-Aware Attention

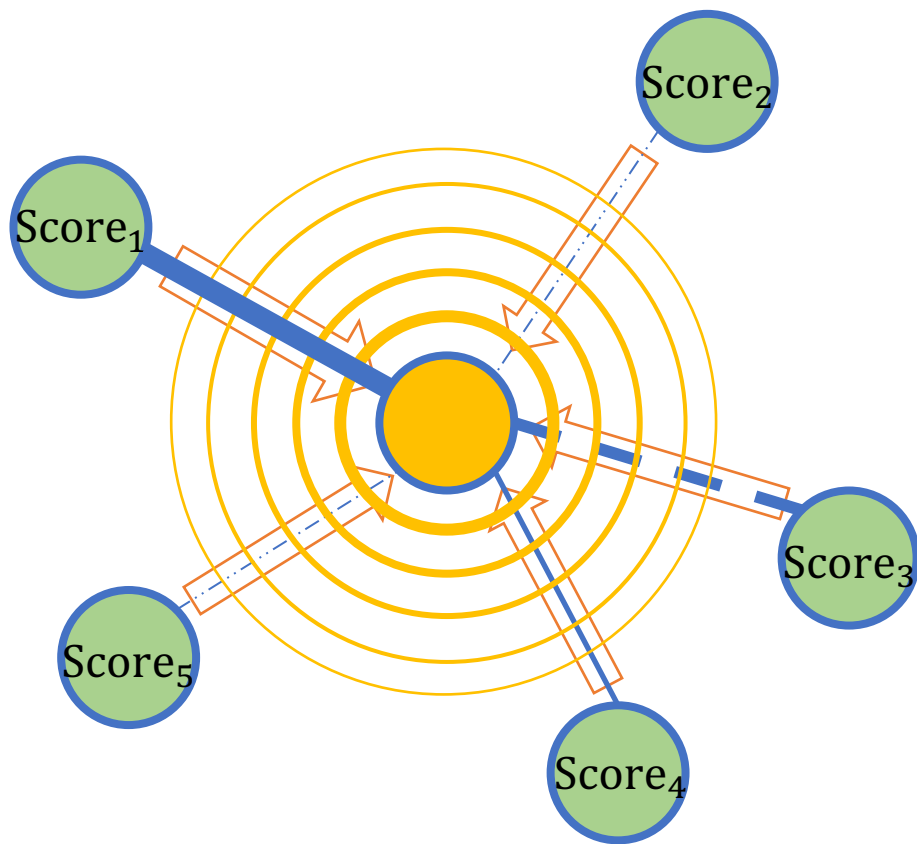
- Model how predicates affect the importance of neighboring entities by using shared self-attention mechanism



$$\alpha_{ij}^{\ell} = \frac{\exp(\sigma_a(\sum_m \vec{a}_{\ell}^T [s^{\ell-1}(i) || \phi(p_{ij}^m) || s^{\ell-1}(j)]))}{\sum_{k \in \mathcal{N}(i) \cup \{i\}} \exp(\sigma_a(\sum_m \vec{a}_{\ell}^T [s^{\ell-1}(i) || \phi(p_{ik}^m) || s^{\ell-1}(k)]))}$$

- α_{ij}^{ℓ} : node i 's attention on node j computed by the ℓ -th layer
- p_{ik}^m : predicate of m -th edge between nodes i and j
- $\phi(\cdot)$: mapping from a predicate to its embedding
- $s^{\ell}(i)$: estimated score of node i
- $\mathcal{N}(i)$: neighbors of node i

Idea 3: Centrality Adjustment



$$c(i) = \log(d(i) + \epsilon)$$
$$c^*(i) = \gamma \cdot c(i) + \beta$$
$$s^*(i) = \sigma_s(c^*(i) \cdot s^L(i))$$

- $d(i)$: in-degree of node i
- $c(i)$: initial centrality of node i
- $c^*(i)$: scaled and shifted centrality of node i
- $s^*(i)$: centrality-adjusted score estimation of node i

Experiments: Evaluation Metrics

- Ranking quality
 - **NDCG** (Normalized Discounted Cumulative Gain)
 - **Spearman** correlation coefficient
- Regression quality
 - **RMSE** (Root-Mean-Squared Error)

Experiments: Datasets

Name	# Nodes	# Edges	# Predicates	Input Score Type	# Nodes w/ Scores	Data for OOD Evaluation
FB15K	14,951	592,213	1,345	# Pageviews	14,108 (94%)	N/A
MUSIC10K	24,830	71,846	10	Song hotttnesss	4,214 (17%)	Artist hotttnesss
TMDB5K	123,906	532,058	22	Movie popularity	4,803 (4%)	Director ranking
IMDB	1,567,045	14,067,776	28	# Votes for movies	215,769 (14%)	Director ranking

Experiments: Evaluation Metrics

- Ranking quality
 - **NDCG** (Normalized Discounted Cumulative Gain)

$$\text{DCG@}k = \sum_{i=1}^k \frac{r_i}{\log_2(i+1)} \quad \text{NDCG@}k = \frac{\text{DCG@}k}{\text{IDCG@}k} \text{ where IDCG@}k \text{ is an ideal DCG at position } k$$

- **Spearman** correlation coefficient

$$\text{Spearman} = \frac{\sum_i (g_{r_i} - \bar{g}_r)(s_{r_i} - \bar{s}_r)}{\sqrt{(\sum_i (g_{r_i} - \bar{g}_r)^2)} \sqrt{(\sum_i (s_{r_i} - \bar{s}_r)^2)}}$$

- r_i : graded relevance of node at position i
- \vec{g}, \vec{s} : ground truth scores and predicted scores
- \vec{g}_r, \vec{s}_r : rankings induced from \vec{g} and \vec{s}
- \bar{g}_r, \bar{s}_r : mean of \vec{g}_r and \vec{s}_r

- Regression quality
 - **RMSE** (Root-Mean-Squared Error)

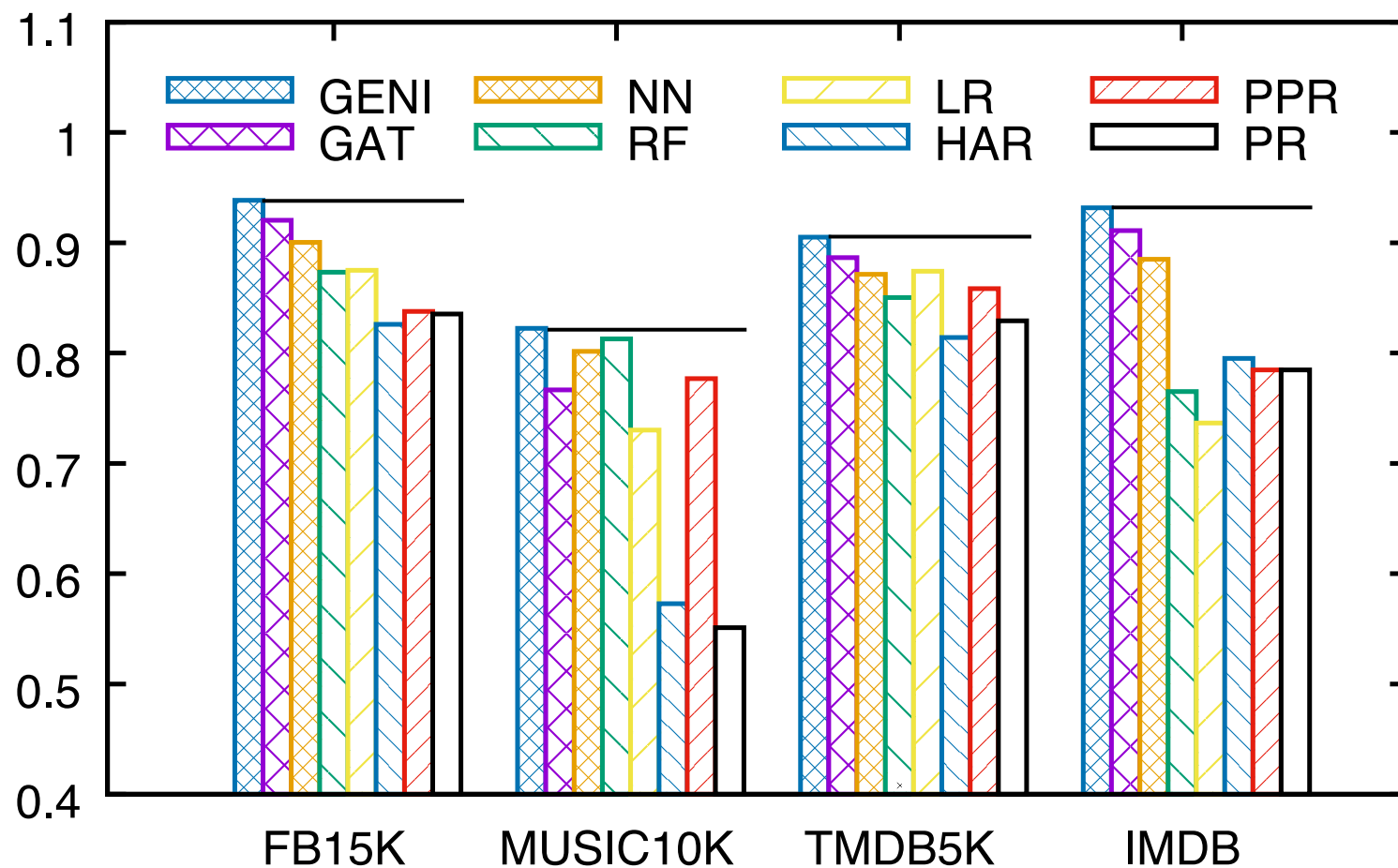
$$\text{RMSE} = \frac{1}{|V_s|} \sum_{i \in V_s} (s(i) - g(i))^2$$

- $s(i)$: predicted score of node i
- $g(i)$: ground truth score of node i
- V_s : a set of nodes with importance scores

In-Domain Evaluation

GENI (blue) outperforms baselines

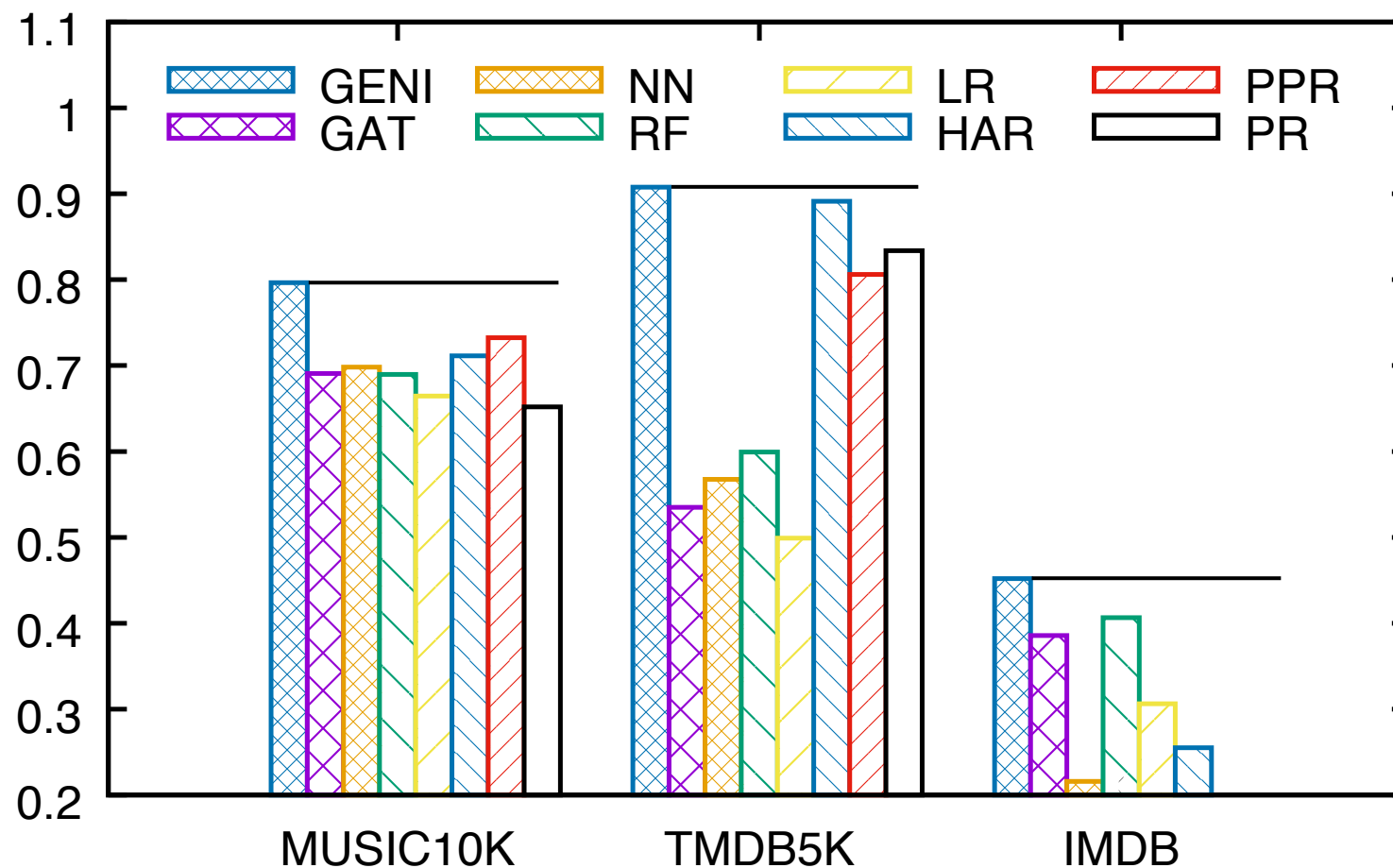
NDCG@100,
higher is
better



Out-Of-Domain Evaluation

GENI (blue) outperforms baselines

NDCG@100,
higher is
better



Experiments: In-Domain Prediction

Method	FB15K		MUSIC10K		TMDB5K		IMDB	
	NDCG@100	SPEARMAN	NDCG@100	SPEARMAN	NDCG@100	SPEARMAN	NDCG@100	SPEARMAN
PR	0.8354 ± 0.016	0.3515 ± 0.015	0.5510 ± 0.021	-0.0926 ± 0.034	0.8293 ± 0.026	0.5901 ± 0.011	0.7847 ± 0.048	0.0881 ± 0.004
PPR	0.8377 ± 0.015	0.3667 ± 0.015	0.7768 ± 0.009	0.3524 ± 0.046	0.8584 ± 0.013	<u>0.7385 ± 0.010</u>	0.7847 ± 0.048	0.0881 ± 0.004
HAR	0.8261 ± 0.005	0.2020 ± 0.012	0.5727 ± 0.017	0.0324 ± 0.044	0.8141 ± 0.021	0.4976 ± 0.014	0.7952 ± 0.036	0.1318 ± 0.005
LR	0.8750 ± 0.005	0.4626 ± 0.019	0.7301 ± 0.023	0.3069 ± 0.032	0.8743 ± 0.015	0.6881 ± 0.013	0.7365 ± 0.009	0.5013 ± 0.002
RF	0.8734 ± 0.005	0.5122 ± 0.019	<u>0.8129 ± 0.012</u>	<u>0.4577 ± 0.012</u>	0.8503 ± 0.016	0.5959 ± 0.022	0.7651 ± 0.010	0.4753 ± 0.005
NN	0.9003 ± 0.005	0.6031 ± 0.012	0.8015 ± 0.017	0.4491 ± 0.027	0.8715 ± 0.006	0.7009 ± 0.009	0.8850 ± 0.016	0.5120 ± 0.008
GAT	<u>0.9205 ± 0.009</u>	<u>0.7054 ± 0.013</u>	0.7666 ± 0.016	0.4276 ± 0.023	<u>0.8865 ± 0.011</u>	0.7180 ± 0.010	<u>0.9110 ± 0.011</u>	<u>0.7060 ± 0.007</u>
GENI	0.9385 ± 0.004	0.7772 ± 0.006	0.8224 ± 0.018	0.4783 ± 0.009	0.9051 ± 0.005	0.7796 ± 0.009	0.9318 ± 0.005	0.7387 ± 0.002

- GENI performs the best for all datasets
- Supervised models mostly outperform non-trainable ones
- Directly utilizing network connectivity further enhances performance

Experiments: Out-Of-Domain Prediction

Method	MUSIC10K		TMDB5K		IMDB	
	NDCG@100	NDCG@2000	NDCG@100	NDCG@2000	NDCG@100	NDCG@2000
PR	0.6520 \pm 0.000	0.8779 \pm 0.000	0.8337 \pm 0.000	0.8079 \pm 0.000	0.0000 \pm 0.000	0.1599 \pm 0.000
PPR	<u>0.7324 \pm 0.006</u>	<u>0.9118 \pm 0.002</u>	0.8060 \pm 0.041	0.7819 \pm 0.022	0.0000 \pm 0.000	0.1599 \pm 0.000
HAR	0.7113 \pm 0.004	0.8982 \pm 0.001	<u>0.8913 \pm 0.010</u>	<u>0.8563 \pm 0.007</u>	0.2551 \pm 0.019	0.3272 \pm 0.005
LR	0.6644 \pm 0.006	0.8667 \pm 0.001	0.4990 \pm 0.013	0.5984 \pm 0.002	0.3064 \pm 0.007	0.2755 \pm 0.003
RF	0.6898 \pm 0.022	0.8796 \pm 0.003	0.5993 \pm 0.040	0.6236 \pm 0.005	<u>0.4066 \pm 0.145</u>	0.3719 \pm 0.040
NN	0.6981 \pm 0.017	0.8836 \pm 0.005	0.5675 \pm 0.023	0.6172 \pm 0.009	0.2158 \pm 0.035	0.3105 \pm 0.019
GAT	0.6909 \pm 0.009	0.8834 \pm 0.003	0.5349 \pm 0.016	0.5999 \pm 0.007	0.3858 \pm 0.065	<u>0.4209 \pm 0.016</u>
GENI	0.7964 \pm 0.007	0.9121 \pm 0.002	0.9078 \pm 0.004	0.8776 \pm 0.002	0.4519 \pm 0.051	0.4962 \pm 0.025

- Prediction is done for entities of some type \mathcal{T} , which is not used for training.
- GENI achieves the best results for all KGs
- Non-trainable methods achieves better results on MUSIC10K and TMDB5K

Experiments: Case Study

Top-10 movies (In-domain estimation)

	GENI		HAR		GAT	
1	The Dark Knight Rises	11	Jason Bourne	63	The Dark Knight Rises	11
2	The Lego Movie	70	The Wolf of Wall Street	21	Clash of the Titans	103
3	Spectre	10	Rock of Ages	278	Ant-Man	4
4	Les Misérables	94	Les Misérables	94	The Lego Movie	68
5	The Amazing Spider-Man	22	The Dark Knight Rises	7	Jack the Giant Slayer	126
6	Toy Story 2	39	V for Vendetta	27	Spectre	7
7	V for Vendetta	26	Now You See Me 2	81	The Wolf of Wall Street	16
8	Clash of the Titans	97	Spectre	5	The 5th Wave	67
9	Ant-Man	-2	Austin Powers in Goldmember	140	The Hunger Games: Mockingjay - Part 2	-4
10	Iron Man 2	29	Alexander	141	X-Men: First Class	767

Top-10 directors (Out-of-domain estimation)

	GENI		HAR		GAT	
1	Steven Spielberg	0	Steven Spielberg	0	Noam Murro	N/A
2	Tim Burton	9	Martin Scorsese	44	J Blakeson	N/A
3	Ridley Scott	6	Ridley Scott	6	Pitof	N/A
4	Martin Scorsese	42	Clint Eastwood	19	Paul Tibbitt	N/A
5	Francis Ford Coppola	158	Woody Allen	112	Rupert Sanders	N/A
6	Peter Jackson	-4	Robert Zemeckis	1	Alan Taylor	145
7	Robert Rodriguez	127	Tim Burton	4	Peter Landesman	N/A
8	Gore Verbinski	8	David Fincher	40	Hideo Nakata	N/A
9	Joel Schumacher	63	Oliver Stone	105	Drew Goddard	N/A
10	Robert Zemeckis	-3	Ron Howard	-2	Tim Miller	N/A

- The top-10 movies predicted by GENI is qualitatively better than others
- The top-10 directors by GENI and HAR are similar in quality, having five common directors
- GAT's estimation on directors is much worse than the two others

Experiments: In-Domain Regression

RMSE of In-Domain Prediction for Supervised Methods

Method	FB15K	MUSIC10K	TMDB5K	IMDB
LR	1.3536 ± 0.017	0.1599 ± 0.002	0.8431 ± 0.028	1.7534 ± 0.005
RF	1.2999 ± 0.024	0.1494 ± 0.002	0.9223 ± 0.015	1.8181 ± 0.011
NN	1.2463 ± 0.015	0.1622 ± 0.009	0.8496 ± 0.012	2.0279 ± 0.033
GAT	1.0798 ± 0.031	0.1635 ± 0.007	0.8020 ± 0.010	1.2972 ± 0.018
GENI	0.9471 ± 0.017	0.1491 ± 0.002	0.7150 ± 0.003	1.2079 ± 0.011

- GENI performs better than other supervised baselines
- Overall, the regression performance of supervised methods follows a similar trend to their performance in terms of ranking measures

Experiments: Flexibility for Centrality Adjustment

Method	FB15K		TMDB5K	
	NDCG@100	SPEARMAN	NDCG@100	SPEARMAN
PR	0.835 ± 0.02	0.352 ± 0.02	0.829 ± 0.03	0.590 ± 0.01
Log In-Degree	0.810 ± 0.02	0.300 ± 0.03	0.852 ± 0.02	0.685 ± 0.02
GENI-Fixed CA	0.868 ± 0.01	0.613 ± 0.01	0.899 ± 0.01	0.771 ± 0.01
GENI-Flexible CA	0.938 ± 0.00	0.777 ± 0.01	0.905 ± 0.01	0.780 ± 0.01

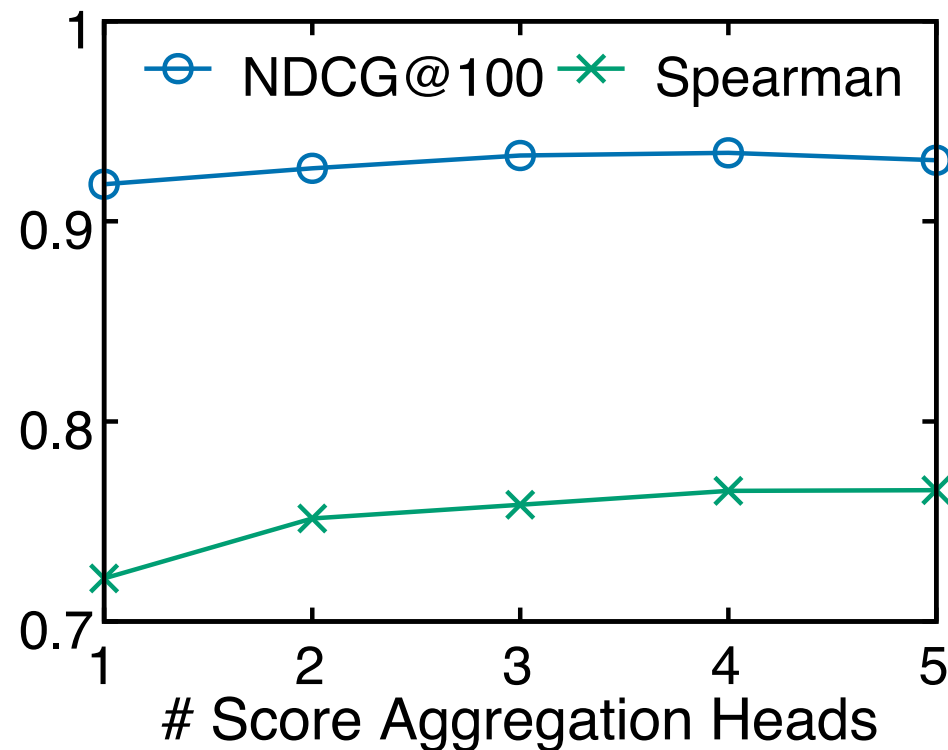
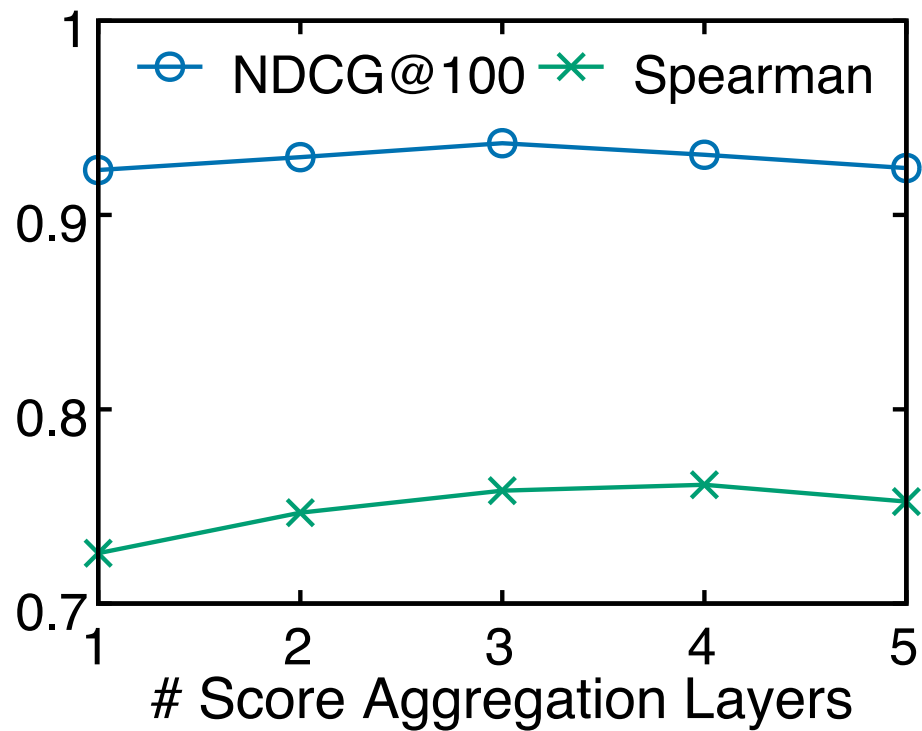
- GENI with fixed CA estimates $s^*(i) = \sigma_s(c(i) \cdot s^L(i))$
- When node centrality correlates well with input scores, fixed CA works well
- When node centrality does not agree with input scores, flexible CA performs much better than fixed CA

Experiments: Effect of Considering Predicates

Metric	Shared Embedding	Distinct Embedding
NDCG@100	0.9062 ± 0.008	0.9385 ± 0.004
SPEARMAN	0.6894 ± 0.007	0.7772 ± 0.006

- Using “shared embedding” forces GENI to lose the ability to distinguish between different predicates
- Results show that GENI makes an effective use of predicates for modeling the relation between node importance

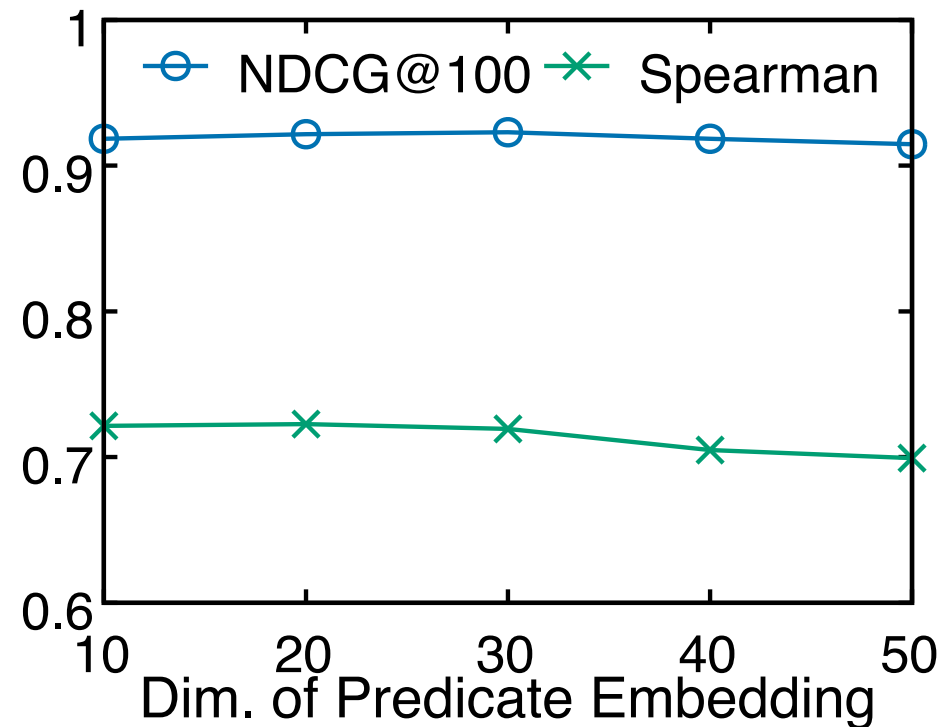
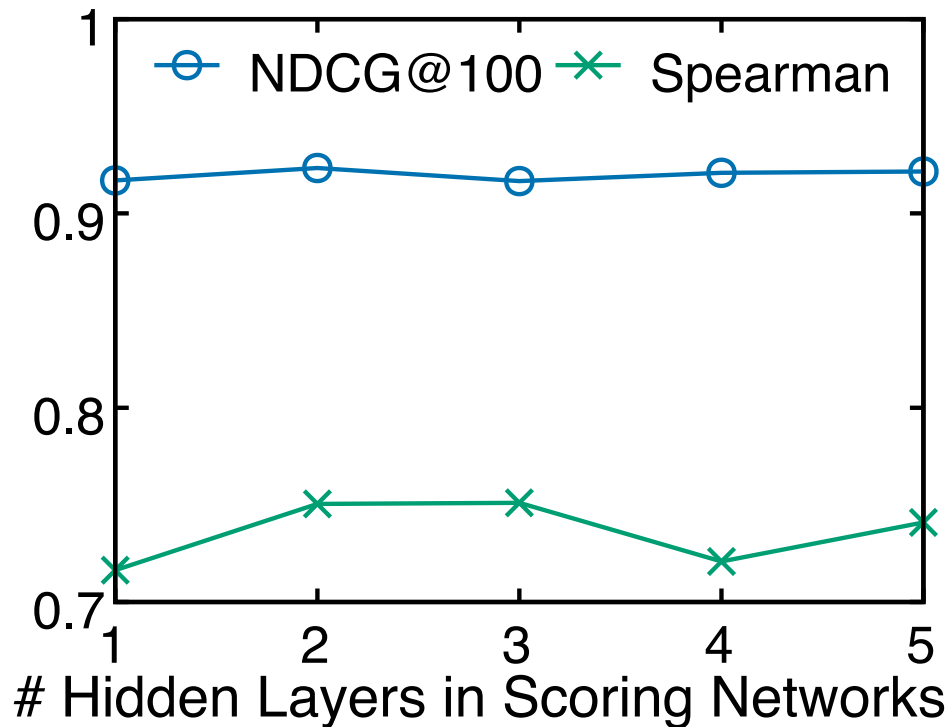
Experiments: Parameter Sensitivity



- Model performance improves as we use a greater number of SA layers and SA heads

Experiments: Parameter Sensitivity

Detail



- Model performance tends to improve as we use a greater number of hidden layers in scoring networks
- Increasing the dimension of predicate embedding beyond an appropriate value negatively affects model performance